



中国科学院大学
University of Chinese Academy of Sciences

计算机科学导论

系统思维-3

无缝衔接

zxu@ict.ac.cn

- 系统思维概述
- 抽象化
- 模块化
- 无缝衔接
 - 扬雄周期原理
 - 指令周期与指令流水线
 - 波斯特尔鲁棒性原理（宽进严出原理）
 - 冯诺依曼穷举原理
 - 阿姆达尔定律

由模块化抽象表达的计算过程
如何能够流畅运行

作业答疑

3. 下述哪个选项正确地描述了计算机的软件抽象？（A）
- (a) 中间件之所以称为中间件，是因为它处于应用软件和操作系统之间。
 - (b) 操作系统是固件，必须存放在硬盘中，因为计算机开机上电以后首先执行操作系统代码。
 - (c) 数据库管理系统是操作系统的一部分。
 - (d) 系统软件就是操作系统。

软件类型			例子
应用软件			科学计算、企业计算、个人计算；办公软件、搜索引擎、微信、抖音
基础软件	中间件	数据库、Web服务器、浏览器、应用框架	MySQL、OceanBase、WebServer.go、Chrome、Safari、TensorFlow
		编程语言及其编译器或解释器	C、Go、JavaScript、Python、shell
	系统软件	操作系统	Linux、安卓Android、iOS、Windows
		固件	BIOS，UEFI

1. 无缝衔接（Seamless Transition）

- 计算过程在全系统中流畅地正确运行，避免缝隙和瓶颈
 - **无缝隙**：相邻的步骤之间的形式与内容（格式与语义）匹配
 - 信息和计算无障碍地从一个模块、步骤过渡到下一个模块、步骤
 - **宽瓶颈**：做不到完全流畅，至少也要控制瓶颈，使系统满足用户体验需求

实现无缝衔接的计算思维原理

- 无缝隙：计算过程归纳法（功能的无缝衔接）

- 确定计算过程第一步骤

- 保证当前步骤正确执行

- 正确地衔接到下一步骤

扬雄周期原理

波斯特尔鲁棒原理

冯诺依曼穷举原理

- 宽瓶颈：性能的无缝衔接

阿姆达尔定律

2. 扬雄周期原理

优于尼采的永恒轮回思想：die ewige Wiederkunft

- 汉代扬雄所著的《太玄经》
 - 《太玄经·周首》：☰ 阳气周神而反乎始，物继其汇
 - 宋代司马光诠释：“岁功既毕，神化既周”

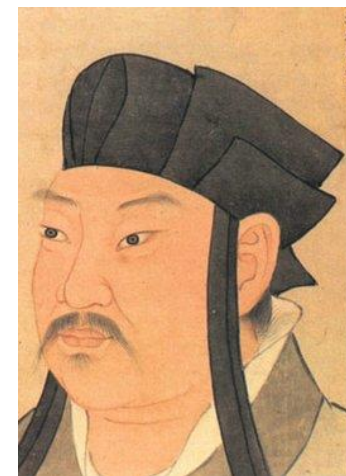
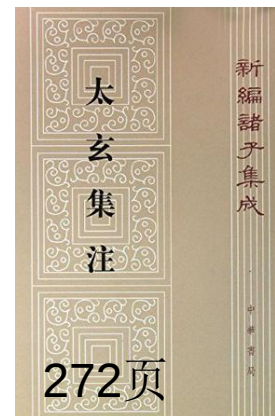
Head Full Circle ☰

Yang qi comes full circle.

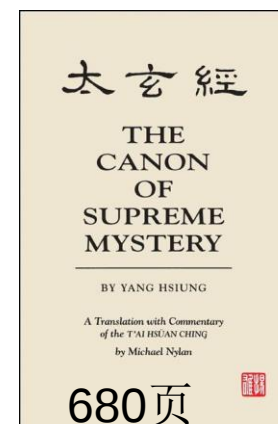
Divinely, it returns to the beginning.

Things go on to preserve their kinds.

- UC-Berkeley戴梅可教授的英文版译注
The Canon of Supreme Mystery by Yang Hsiung
- 创新型人才需要领悟思维
 - 什么是周期的本质？为什么要有周期？



扬雄，前53年-18年
三进制《太玄经》

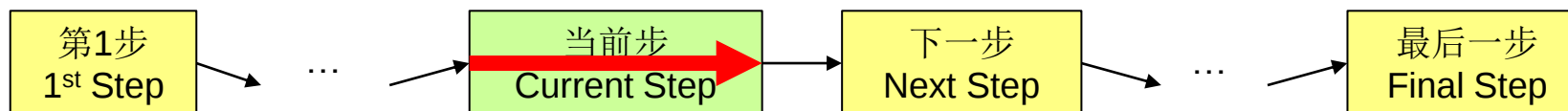


扬雄周期原理

优于尼采的永恒轮回：die ewige Wiederkunft

- 汉代扬雄所著的《太玄经》
 - 《太玄经•周首》：“阳气周神而反乎始，物继其汇”
 - 宋代司马光诠释道：“岁功既毕，神化既周”
 - 三个要点
 - 岁功既毕：当前步骤执行完毕
 - 周而复始：哪个步骤的开始？

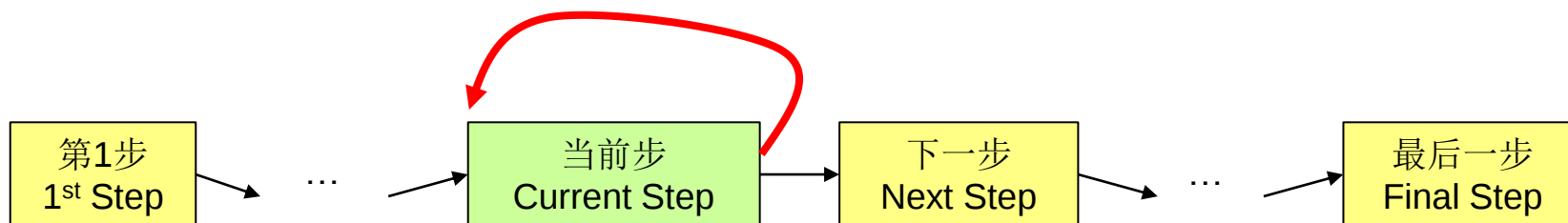
计算过程运行时的动态步骤序列



扬雄周期原理

优于尼采的永恒轮回：die ewige Wiederkunft

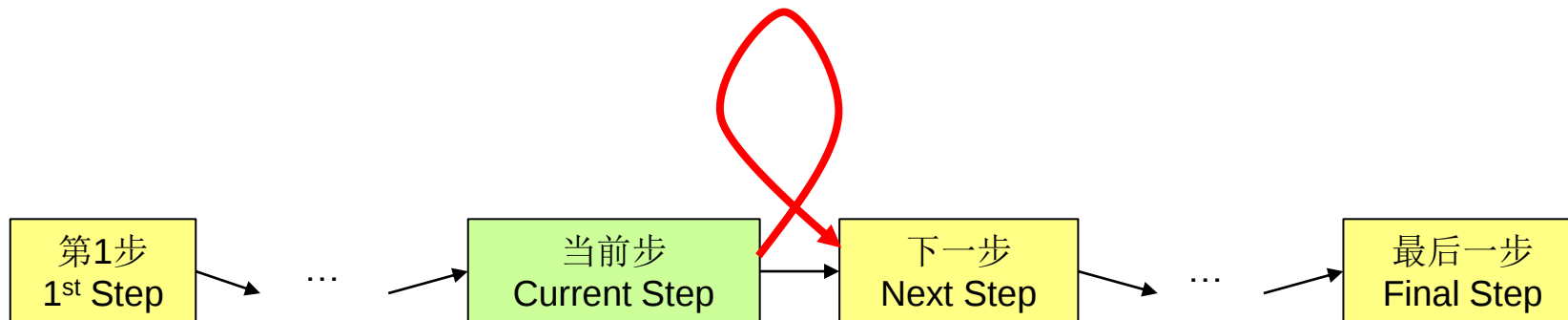
- 汉代扬雄所著的《太玄经》
 - 《太玄经•周首》：“阳气周神而反乎始，物继其汇”
 - 宋代司马光诠释道：“岁功既毕，神化既周”
 - 三个要点
 - 岁功既毕：当前步骤执行完毕
 - 周而复始：哪个步骤的开始？**是当前步骤的开始吗？**



扬雄周期原理

优于尼采的永恒轮回：die ewige Wiederkunft

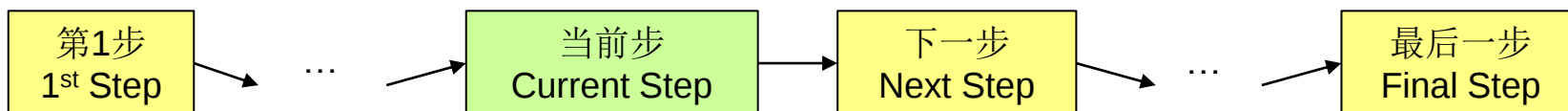
- 汉代扬雄所著的《太玄经》
 - 《太玄经•周首》：“阳气周神而反乎始，物继其汇”
 - 宋代司马光诠释道：“岁功既毕，神化既周”
 - 三个要点
 - 岁功既毕：当前步骤执行完毕
 - 周而复始：**下一步骤的开始！**



扬雄周期原理

优于尼采的永恒轮回：die ewige Wiederkunft

- 汉代扬雄所著的《太玄经》
 - 《太玄经•周首》：“阳气周神而反乎始，物继其汇”
 - 宋代司马光诠释道：“岁功既毕，神化既周”
 - 三个要点
 - 岁功既毕：当前步骤执行完毕
 - 周而复始（哪个步骤的开始？下一步骤的开始）
 - 物继其类（周期原理支持多样性，每个步骤呈现其特色）
 - 指令周期支持各种指令：加法、乘法、存数、跳转等等
 - 指令**译码**：确定当前指令的功能，并定位下一条指令



周期有不同粒度

- 执行完一个XX周期，周而复始执行下一个XX周期
 - 计算过程由**程序**周期组合而成
 - 程序周期由**指令**周期组合而成
 - 指令周期由**时钟**周期组合而成

周期有不同粒度

- 执行完一个XX周期，周而复始执行下一个XX周期
 - 计算过程由**程序**周期组合而成
 - 程序周期由**指令**周期组合而成
 - 指令周期由**时钟**周期组合而成
- 一个时钟周期的操作对应于一个自动机变换
 - 等同于时序电路的一个时钟周期的操作

3. 指令周期与指令流水线

- 处理器的核心是指令流水线

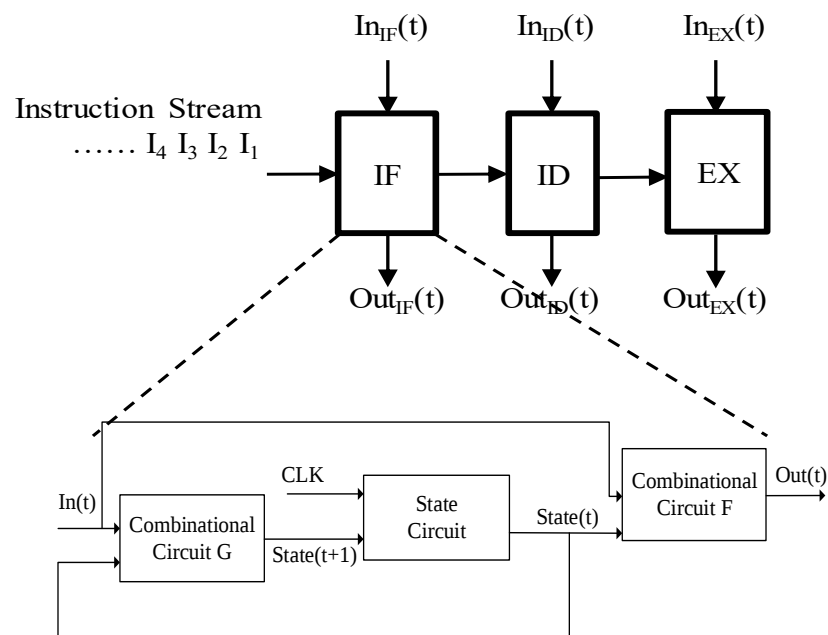
- 指令流水线的每一级是一个时序电路

- 例子：三级指令流水线

- 一个指令周期包含三个步骤（三级）
取指、译码、执行

- 例子：三级指令流水线
执行指令 `MOV 0, R1`

- **Instruction Fetch (IF)** stage: $IR \leftarrow M[PC]$
 - 将内存单元 $M[PC]$ 的指令取到指令寄存器 IR
- **Instruction Decode (ID)**: $\text{Control Signals} = \text{Decode}(IR)$
 - 从指令产生控制信号
- **Instruction Execute (EX)**: $R1 \leftarrow 0; PC \leftarrow PC+1$
 - 根据控制信号执行指令操作，并将程序计数器增量



取指 (IF)

译码 (ID)

执行 (EX)

指令周期与指令流水线

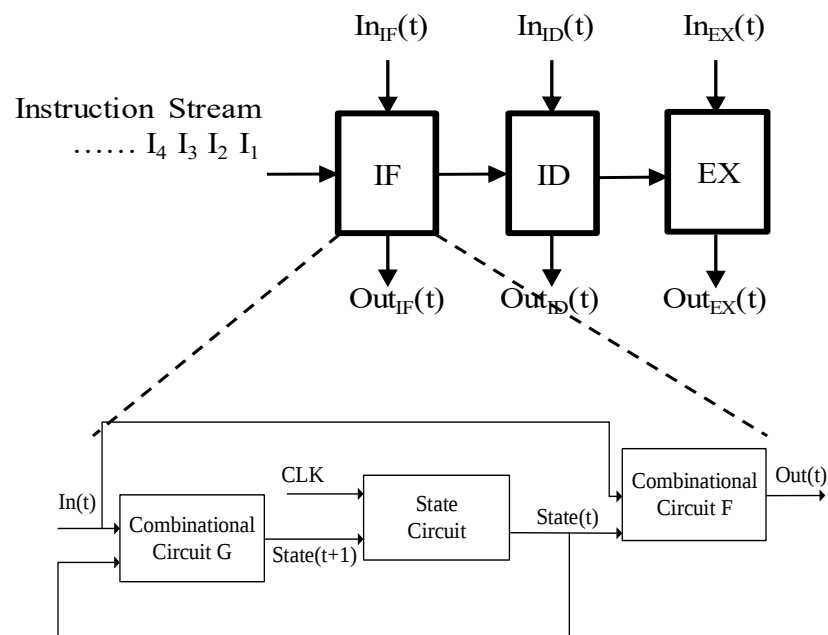
- 处理器的核心是指令流水线

- 指令流水线的每一级是一个时序电路

- 真实处理器的指令流水线有5~31级

- 例子：三级指令流水线
执行指令MOV 0, R1

- **Instruction Fetch (IF)** stage: $IR \leftarrow M[PC]$
 - 将内存单元M[PC]的指令取到指令寄存器IR
- **Instruction Decode (ID)**: $\text{Control Signals} = \text{Decode}(IR)$
 - 从指令产生控制信号
- **Instruction Execute (EX)**: $R1 \leftarrow 0; PC \leftarrow PC+1$
 - 根据控制信号执行指令操作，并将程序计数器增量



取指 (IF)

译码 (ID)

执行 (EX)

3.1 设计斐波那契计算机的指令集

- 继续英文教科书2.3节内容

```
fib[0] = 0      MOV 0, R1
fib[1] = 1      MOV R1, M[R0]           //R0=12 initially
               MOV 1, R1
               MOV R1, M[R0+8]
for i := 2; i < 51; i++ {
  fib[i] = fib[i-1] + fib[i-2]
  MOV 2, R2           // i:=2
  MOV 0, R1           // label Loop
  ADD M[R0+R2*8-16], R1
  ADD M[R0+R2*8-8], R1
  MOV R1, M[R0+R2*8-0]
  INC R2              // i++
  CMP 51, R2          // i < 51?
  JL Loop             // if Yes, goto Loop
}
```

- Design an instruction set for FC
 - Any instruction consists of an **opcode** and one or more **operands**
 - 每条指令包含一个**操作码**和若干**操作数**
 - In mnemonics, e.g., **MOV 0, R1** 汇编语言记号表达
 - In binary, e.g., **000 000000 01** 二进制表达

指令集设计过程

- **初始条件**: 给定汇编语言代码
- **步骤1**: 确定（可见的）存储器与寄存器
 - **FLAGS**: CPU status register **状态寄存器**
 - Holding status value of instruction execution, such as if the result is overflow, zero, less than, etc.
 - Only “less than” is used in this example
 - **PC**: program counter **程序计数器**
 - Holding the address of the next instruction to be executed
 - **R0, R1, and R2**: general purpose registers
三个**通用寄存器**
 - Holding operands of instructions
- **步骤2**: 合并同类指令，确定操作码
 - 合并同类指令，例如，
 - **MOV 0, R1**
 - **MOV 1, R1**
 - **MOV 2, R2**

```
fib[0] = 0          MOV 0, R1  
                   MOV R1, M[R0]  
fib[1] = 1          MOV 1, R1  
                   MOV R1, M[R0+8]  
for i := 2; i < 51; i++ {  
    fib[i] = fib[i-1] + fib[i-2]  MOV 2, R2  
                                MOV 0, R1    // Loop  
                                ADD M[R0+R2*8-16], R1  
                                ADD M[R0+R2*8-8], R1  
                                MOV R1, M[R0+R2*8-0]  
                                INC R2  
                                CMP 51, R2  
                                JL Loop  
}
```

指令集设计过程：步骤2

- FC has a memory and five registers
 - FLAGS, PC, R0, R1, and R2
- Determine the types of instructions and decide the opcodes (one for a type)
 - Merge similar instructions into a type
合并同类指令，如 MOV 0, R1; MOV 1, R1; MOV 2, R2
 - E.g., 3 instructions move an immediate value to a register
 - MOV 0, R1; MOV 1, R1; MOV 2, R2
 - They belong to one type of instruction
- There are six types of instructions, needing 3 bits to specify
6种指令，需要3比特操作码

```
fib[0] = 0
fib[1] = 1
for i := 2; i < 51; i++ {
    fib[i] = fib[i-1] + fib[i-2]
}
```

```
MOV 0, R1
MOV R1, M[R0]
MOV 1, R1
MOV R1, M[R0+8]
MOV 2, R2
MOV 0, R1 // Loop
ADD M[R0+R2*8-16], R1
ADD M[R0+R2*8-8], R1
MOV R1, M[R0+R2*8-0]
INC R2
CMP 51, R2
JL Loop
```

Instruction Type	Opcode	Semantics 指令语义
MOV to Register	000	Assign an immediate value to a register
MOV to Memory	001	Assign the content of a register to M[Address]
ADD	010	$R1 + M[Address] \rightarrow R1$
INC	011	$R + 1 \rightarrow R$ (R is a register)
CMP	100	Compare to a value, assign the result to FLAGS
JL	101	If FLAGS is '<' (less than), Loop $\rightarrow$ PC

指令集设计过程：步骤2

- FC has a memory and five registers
 - FLAGS, PC, R0, R1, and R2
- Determine the types of instructions and decide the opcodes
 - Merge similar instructions into a type
 - E.g., 3 instructions move an immediate value to a register
 - MOV 0, R1; MOV 1, R1; MOV 2, R2
 - They belong to one type of instruction
- There are six types of instructions

```
fib[0] = 0          MOV 0, R1
                    MOV R1, M[R0] ✓
fib[1] = 1          MOV 1, R1
                    MOV R1, M[R0+8] ✓
for i := 2; i < 51; i++ {
    fib[i] = fib[i-1] + fib[i-2]
                    MOV 2, R2
                    MOV 0, R1    // Loop
                    ADD M[R0+R2*8-16], R1
                    ADD M[R0+R2*8-8], R1
                    MOV R1, M[R0+R2*8-0] ✓
                    INC R2
                    CMP 51, R2
                    JL Loop
}
```

Instruction Type	Opcode	Semantics
MOV to Register	000	Assign an immediate value to a register
MOV to Memory	001	Assign the content of a register to M[Address]
ADD	010	$R1 + M[\text{Address}] \rightarrow R1$
INC	011	$R + 1 \rightarrow R$ (R is a register)
CMP	100	Compare to a value, assign the result to FLAGS
JL	101	If FLAGS is '<' (less than), Loop $\rightarrow$ PC

指令集设计过程：步骤2

- FC has a memory and five registers
 - FLAGS, PC, R0, R1, and R2
- Determine the types of instructions and decide the opcodes
 - Merge similar instructions into a type
 - E.g., 3 instructions move an immediate value to a register
 - MOV 0, R1; MOV 1, R1; MOV 2, R2
 - They belong to one type of instruction
- There are six types of instructions

```
fib[0] = 0          MOV 0, R1
                    MOV R1, M[R0] ✓
fib[1] = 1          MOV 1, R1
                    MOV R1, M[R0+8] ✓
for i := 2; i < 51; i++ {
    fib[i] = fib[i-1] + fib[i-2]
                    MOV 2, R2
                    MOV 0, R1    // Loop
                    ADD M[R0+R2*8-16], R1 ✓
                    ADD M[R0+R2*8-8], R1 ✓
                    MOV R1, M[R0+R2*8-0] ✓
                    INC R2
                    CMP 51, R2
                    JL Loop
}
```

Instruction Type	Opcode	Semantics
MOV to Register	000	Assign an immediate value to a register
MOV to Memory	001	Assign the content of a register to M[Address]
ADD	010	$R1 + M[Address] \rightarrow R1$
INC	011	$R + 1 \rightarrow R$ (R is a register)
CMP	100	Compare to a value, assign the result to FLAGS
JL	101	If FLAGS is '<' (less than), Loop $\rightarrow$ PC

指令集设计过程：步骤2

- FC has a memory and five registers
 - FLAGS, PC, R0, R1, and R2
- Determine the types of instructions and decide the opcodes
 - Merge similar instructions into a type
 - E.g., 3 instructions move an immediate value to a register
 - MOV 0, R1; MOV 1, R1; MOV 2, R2
 - They belong to one type of instruction
- There are six types of instructions

```
fib[0] = 0      MOV 0, R1
                MOV R1, M[R0] ✓
fib[1] = 1      MOV 1, R1
                MOV R1, M[R0+8] ✓
for i := 2; i < 51; i++ {
    fib[i] = fib[i-1] + fib[i-2]
                MOV 2, R2
                MOV 0, R1    // Loop
                ADD M[R0+R2*8-16], R1 ✓
                ADD M[R0+R2*8-8], R1 ✓
                MOV R1, M[R0+R2*8-0] ✓
                INC R2 ✓
                CMP 51, R2
                JL Loop
}
```

Instruction Type	Opcode	Semantics
MOV to Register	000	Assign an immediate value to a register
MOV to Memory	001	Assign the content of a register to M[Address]
ADD	010	$R1 + M[Address] \rightarrow R1$
INC	011	$R + 1 \rightarrow R$ (R is a register)
CMP	100	Compare to a value, assign the result to FLAGS
JL	101	If FLAGS is '<' (less than), Loop $\rightarrow$ PC

指令集设计过程：步骤2

- FC has a memory and five registers
 - FLAGS, PC, R0, R1, and R2
- Determine the types of instructions and decide the opcodes
 - Merge similar instructions into a type
 - E.g., 3 instructions move an immediate value to a register
 - MOV 0, R1; MOV 1, R1; MOV 2, R2
 - They belong to one type of instruction
- There are six types of instructions

```
fib[0] = 0      MOV 0, R1
                MOV R1, M[R0] ✓
fib[1] = 1      MOV 1, R1
                MOV R1, M[R0+8] ✓
for i := 2; i < 51; i++ {
    fib[i] = fib[i-1] + fib[i-2]
                MOV 2, R2
                MOV 0, R1    // Loop
                ADD M[R0+R2*8-16], R1 ✓
                ADD M[R0+R2*8-8], R1 ✓
                MOV R1, M[R0+R2*8-0] ✓
                INC R2 ✓
                CMP 51, R2 ✓
            }
                JL Loop
```

Instruction Type	Opcode	Semantics
MOV to Register	000	Assign an immediate value to a register
MOV to Memory	001	Assign the content of a register to M[Address]
ADD	010	$R1 + M[Address] \rightarrow R1$
INC	011	$R + 1 \rightarrow R$ (R is a register)
CMP	100	Compare to a value, assign the result to FLAGS
JL	101	If FLAGS is '<' (less than), Loop $\rightarrow$ PC

指令集设计过程：步骤2

- FC has a memory and five registers
 - FLAGS, PC, R0, R1, and R2
- Determine the types of instructions and decide the opcodes
 - Merge similar instructions into a type
 - E.g., 3 instructions move an immediate value to a register
 - MOV 0, R1; MOV 1, R1; MOV 2, R2
 - They belong to one type of instruction
- There are six types of instructions

```
fib[0] = 0          MOV 0, R1
                    MOV R1, M[R0] ✓
fib[1] = 1          MOV 1, R1
                    MOV R1, M[R0+8] ✓
for i := 2; i < 51; i++ {
    fib[i] = fib[i-1] + fib[i-2]
                    MOV 2, R2
                    MOV 0, R1 // Loop
                    ADD M[R0+R2*8-16], R1 ✓
                    ADD M[R0+R2*8-8], R1 ✓
                    MOV R1, M[R0+R2*8-0] ✓
                    INC R2 ✓
                    CMP 51, R2 ✓
                    JL Loop ✓
}
```

Instruction Type	Opcode	Semantics
MOV to Register	000	Assign an immediate value to a register
MOV to Memory	001	Assign the content of a register to M[Address]
ADD	010	$R1 + M[\text{Address}] \rightarrow R1$
INC	011	$R + 1 \rightarrow R$ (R is a register)
CMP	100	Compare to a value, assign the result to FLAGS
JL	101	If FLAGS is '<' (less than), Loop $\rightarrow$ PC

步骤3：确定操作数

- FC has a memory and five registers
 - FLAGS, PC, R0, R1, and R2
- Determine the types of instructions and decide the opcodes
- For each opcode, determine its operands
 - Assuming the instruction length = 11 bits
 - There are 3 data registers, needing 2 bits
 - Leave 6 bits for immediate value
 - The base+index+offset mode
 - Address = $R0 + R2 * I + J$, where
 - R0, R2 are fixed
 - $I = 0, 1, 2, 4, 8$
 - $J = 0, \pm 4, \pm 8, \pm 16$
 - $5 \times 7 = 35$ possible (I, J) pairs
 - $35 < 2^6$, 6 bits are enough
- Notes
 - For INC R2, operand 1 is not used
 - JL has only one operand

确定操作数

In practice, assume 8, 16, 32 or 64 bits

```
fib[0] = 0      MOV 0, R1
                MOV R1, M[R0]
fib[1] = 1      MOV 1, R1
                MOV R1, M[R0+8]
for i := 2; i < 51; i++ {
    fib[i] = fib[i-1] + fib[i-2]
                MOV 2, R2
                MOV 0, R1    // Loop
                ADD M[R0+R2*8-16], R1
                ADD M[R0+R2*8-8], R1
                MOV R1, M[R0+R2*8-0]
                INC R2
                CMP 51, R2
            }
                JL Loop
```

Opcode 3-bit	Operand 1 Immediate Value, 6-bit	Operand 2 Register, 2-bit	Instruction
000	000000	01	MOV 0, R1
000	000001	01	MOV 1, R1
000	000010	10	MOV 2, R2
011		10	INC R2
100	110011	10	CMP 51, R2
101	00000101		JL Loop

Opcode 3-bit	Operand 1 Memory Address, 6-bit	Operand 2 Register, 2-bit	Instruction
001	$R0 + R2 * 0 + 0$	01	MOV R1, M[R0]
001	$R0 + R2 * 0 + 8$	01	MOV R1, M[R0+8]
001	$R0 + R2 * 0 - 0$	01	MOV R1, M[R0+R2*8-0]
010	$R0 + R2 * 8 - 8$	01	ADD M[R0+R2*8-8], R1
010	$R0 + R2 * 8 - 16$	01	ADD M[R0+R2*8-16], R1

3.2 一条指令在处理器内部是如何执行的？

- To see an example of executing instruction **MOV 0, R1**

- by a **3-stage instruction pipeline**

三级指令流水线

- Instruction Fetch (IF): $IR \leftarrow M[PC]$
- Instruction Decode (ID): Signals = Decode(IR)
- Instruction Execute (EX): $R1 \leftarrow 0; PC \leftarrow PC + 1$

取指

译码

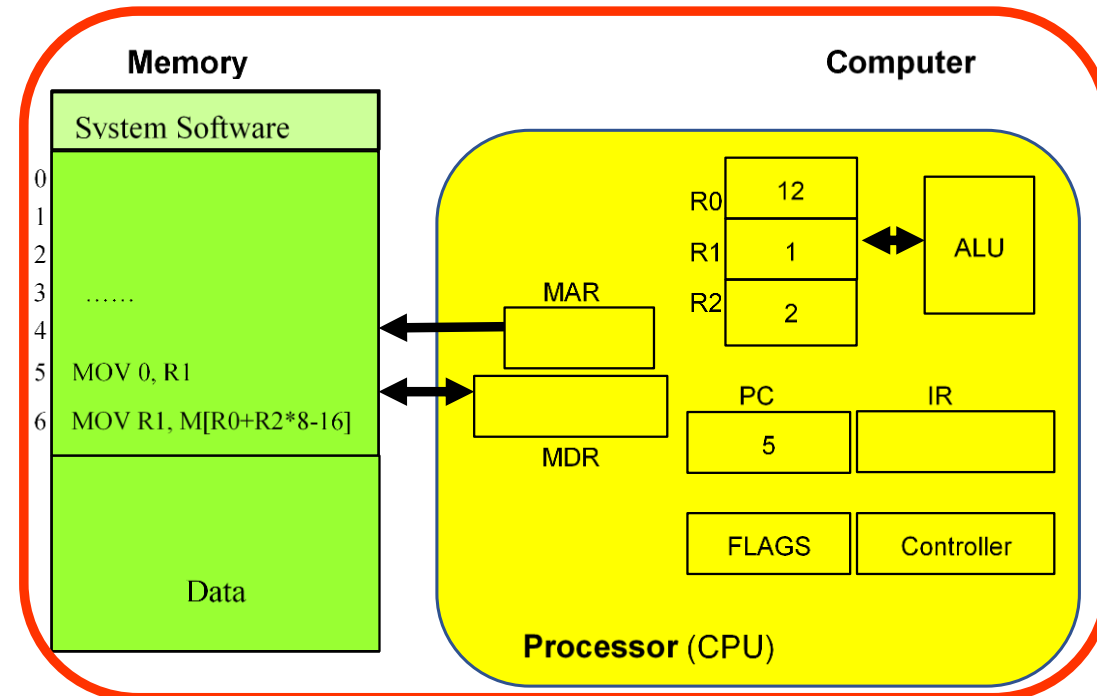
执行

- Internal components

not visible to user

需要关心内部部件（不可见）

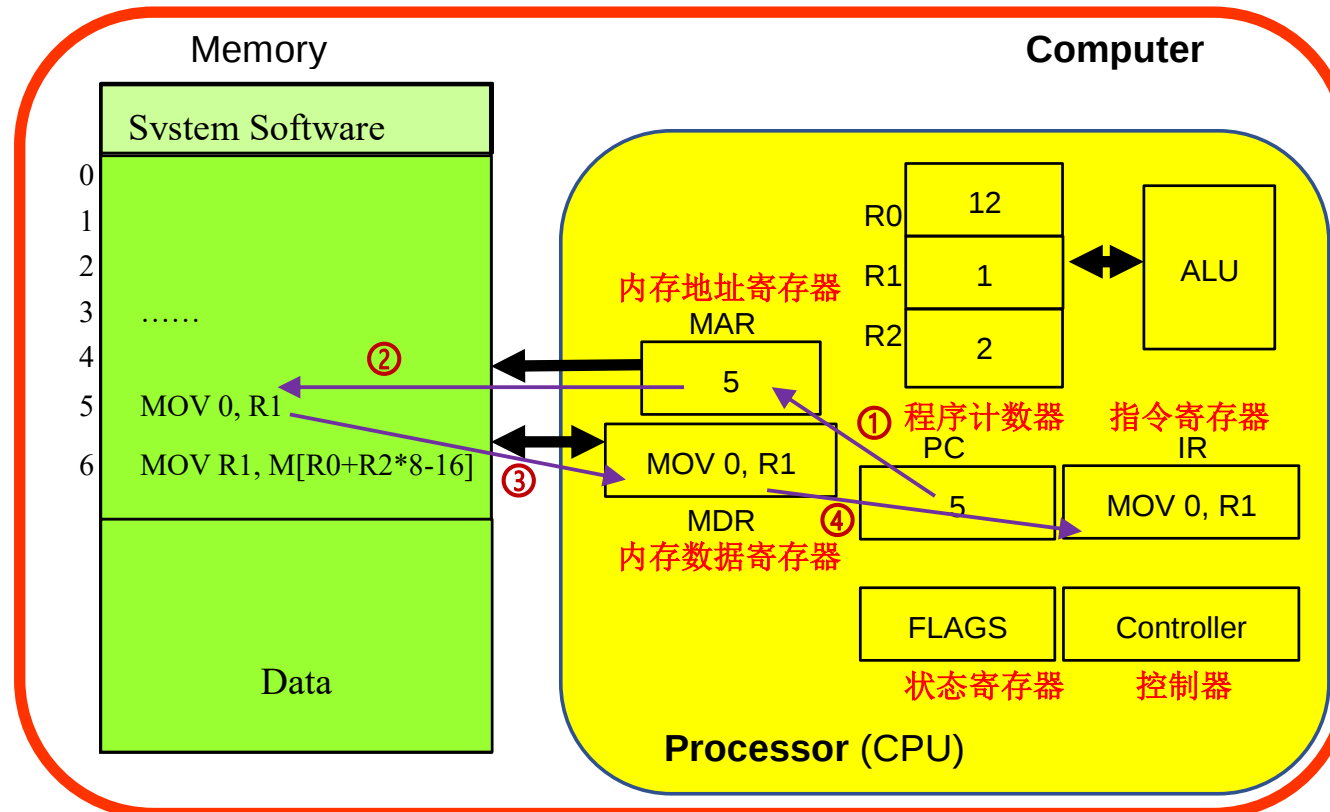
- **IR**: Instruction Register holding the instruction being executed
- **MAR**: Memory Address Register, holding the memory address used
- **MDR**: Memory Data Register, holding the data for a load or store
- **Controller**: control circuit to generate control signals



Execution details

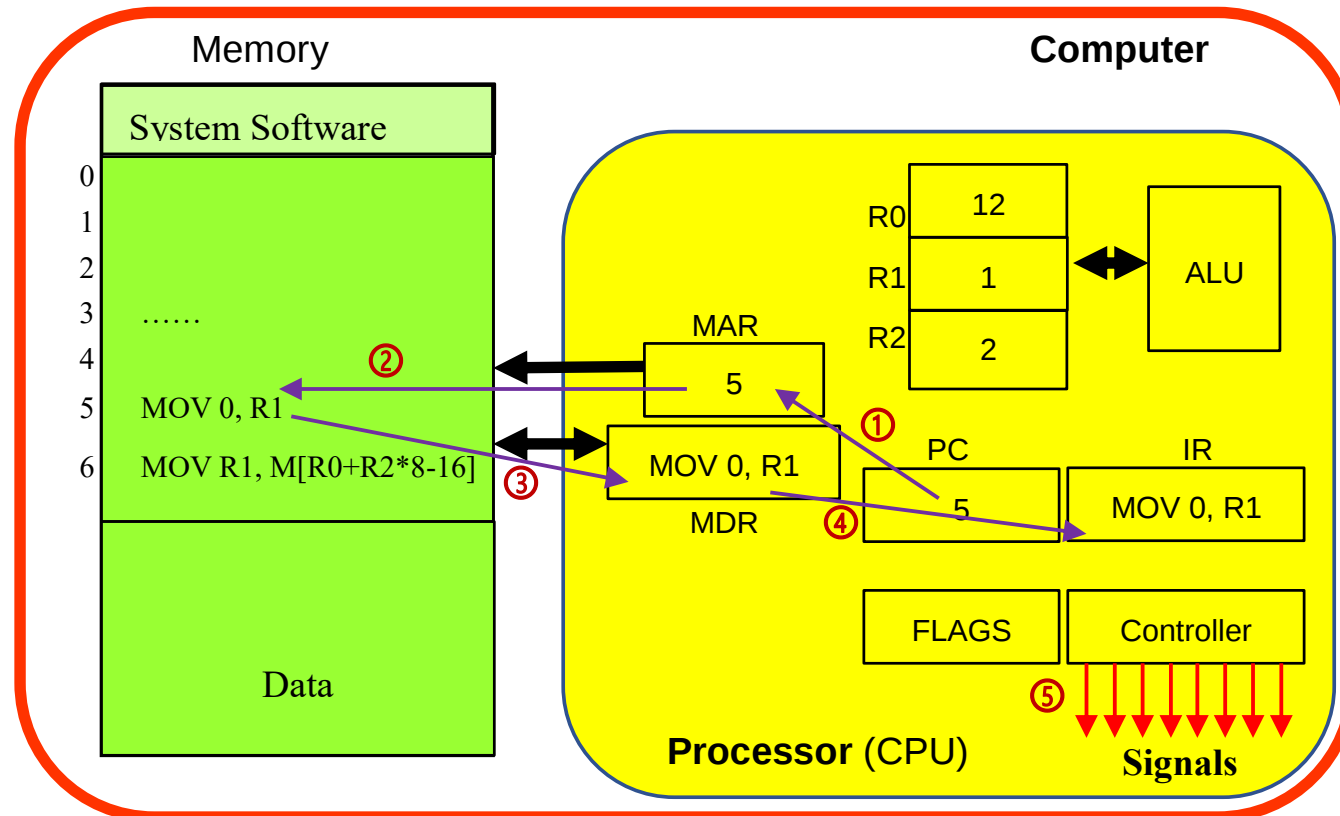
- Instruction Fetch (IF): $IR \leftarrow M[PC]$
 - Instruction Decode (ID): Signals = Decode(IR)
 - Instruction Execute (EX): $R1 \leftarrow 0; PC \leftarrow PC+1$
- IF stage (micro operations ①②③④)

取指



- Instruction Fetch (IF): $IR \leftarrow M[PC]$
 - Instruction Decode (ID): $Signals = Decode(IR)$
 - Instruction Execute (EX): $R1 \leftarrow 0; PC \leftarrow PC+1$
- IF stage (micro operations ①②③④)
 - ID stage (micro operation ⑤)

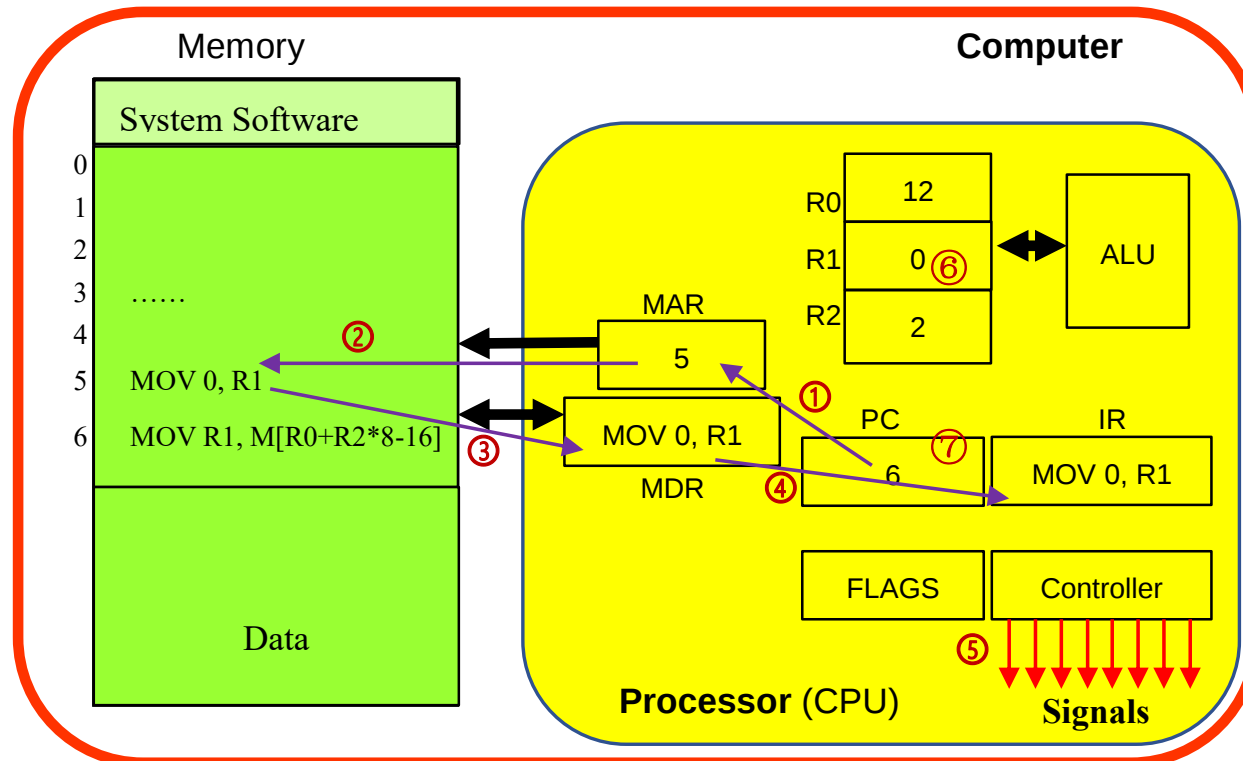
取指
译码



译码:
控制器从
IR的当前
指令产生
控制信号

- Instruction Fetch (IF): $IR \leftarrow M[PC]$
 - Instruction Decode (ID): $Signals = Decode(IR)$
 - Instruction Execute (EX): $R1 \leftarrow 0; PC \leftarrow PC+1$
- IF stage (micro operations ①②③④)
 - ID stage (micro operation ⑤)
 - EX stage (micro operations ⑥⑦)
 - $0 \rightarrow R1; PC+1 \rightarrow PC$

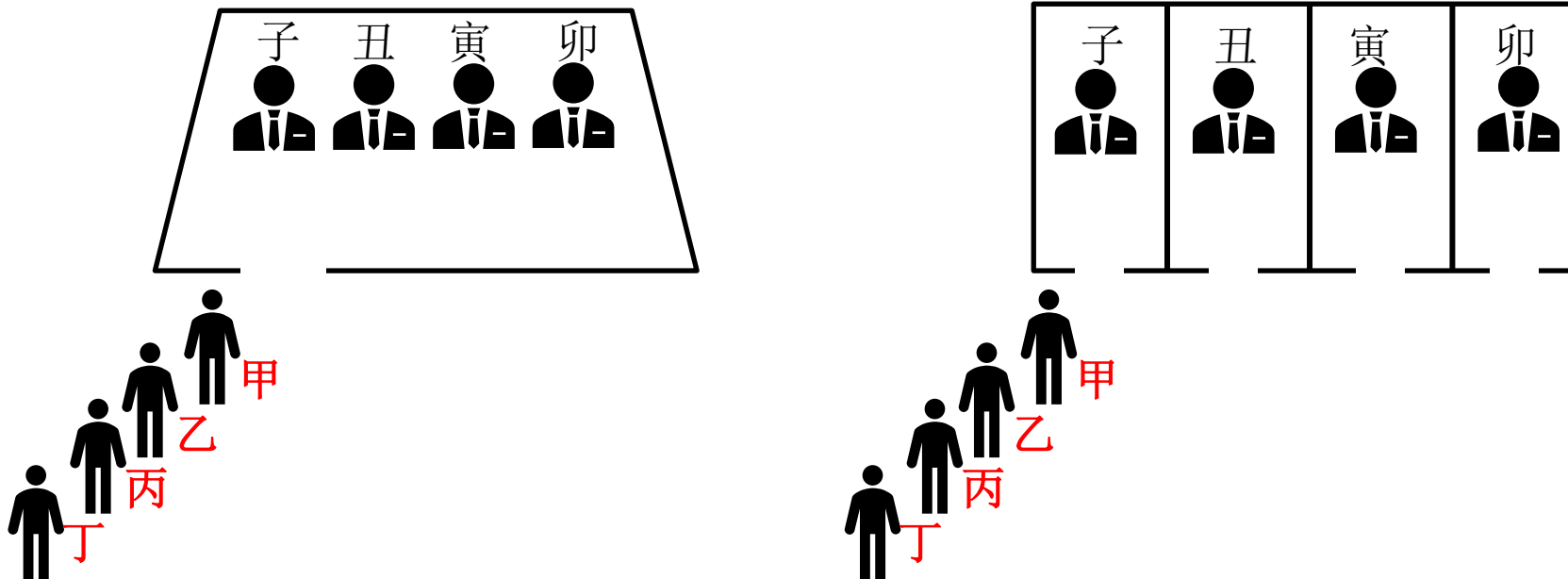
取指
译码
执行



执行:
控制信号驱动相关
部件, 例如使能相
关MUX, 执行指令
要求的操作
 $0 \rightarrow R1$
 $PC+1 \rightarrow PC$

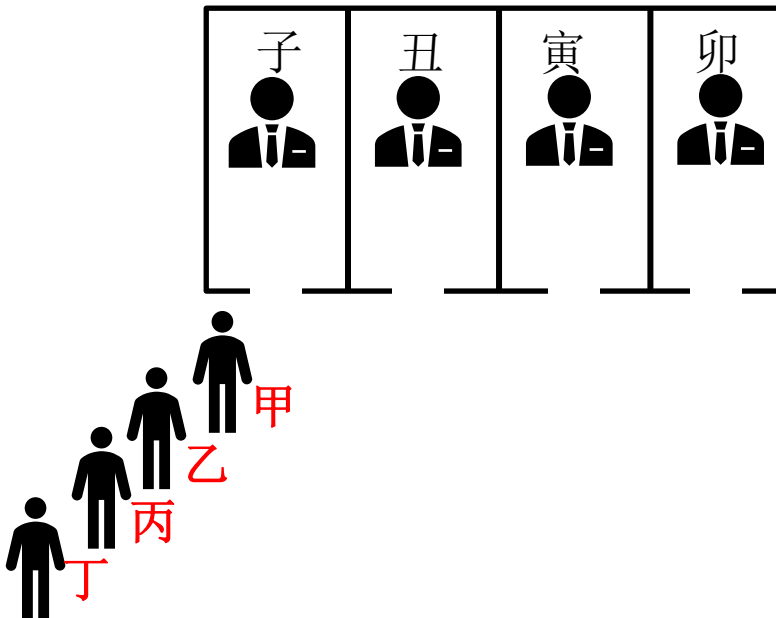
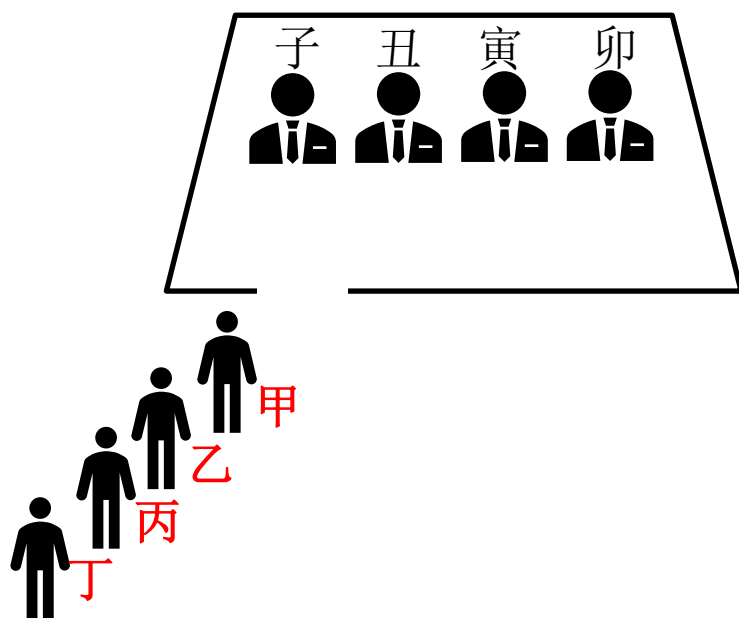
3.3 多条指令的重叠执行（overlapping）

- 用一个例子阐述多条指令的重叠执行
 - 甲乙丙丁4位同学面试研究生，由子丑寅卯4位老师面试。针对每个同学，每位老师有3分钟问答时间。考虑两种面试方式。
 - 方式1.子丑寅卯4位老师在一间面试室里，4位同学依次面试。每位同学一共耗时12分钟。4位同学总计面试时间为： $4 \times (3 \times 4) = 48$ 分钟。
 - 方式2.子丑寅卯4位老师在相邻的4间办公室里，4位同学依次到每位老师办公室面试。每位同学仍然一共耗时12分钟。4位同学总计面试时间是多少？



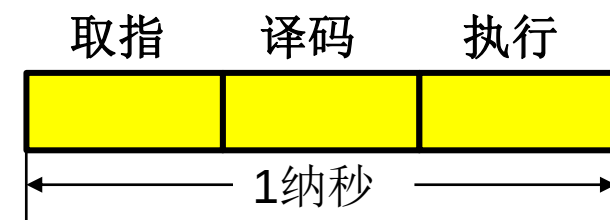
多条指令的重叠执行（overlapping）

- 用一个例子阐述多条指令的重叠执行
 - 甲乙丙丁4位同学面试研究生，由子丑寅卯4位老师面试。针对每个同学，每位老师有3分钟问答时间。考虑两种面试方式。
 - 方式1.子丑寅卯4位老师在一间面试室里，4位同学依次面试。每位同学一共耗时12分钟。4位同学总计面试时间为： $4 \times (3 \times 4) = 48$ 分钟。
 - 方式2.子丑寅卯4位老师在相邻的4间办公室里，4位同学依次到每位老师办公室面试。每位同学仍然一共耗时12分钟。4位同学总计面试时间是多少？
 - 假如有100名同学参加面试呢？



低效情况：多条指令没有重叠执行

- 每个指令周期包含三个操作阶段（微操作），耗时1纳秒
 - 例如，执行指令MOV R1, M[R0] 的三步骤如下：
 - 取指操作：IR $\leftarrow$ M(PC); PC $\leftarrow$ PC+1
 - 译码操作：Signals = Decode(IR)
 - 执行操作：M[R0] $\leftarrow$ R1
- 两个指令周期在指令流水线中并不重叠（no overlapping）
 - 每条指令的执行**独占**指令流水线



峰值速度为1 GIPS
即每秒10亿条指令

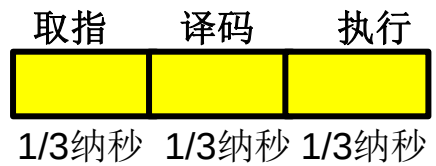


指令流水线机制总是利用重叠（overlap）

处理器主频= 3 GHz，指令流水线同时执行三条指令，平均每个时钟周期执行完毕一条指令

峰值速度：3 Giga Instructions Per Second (GIPS)，即每秒执行30亿条指令

- 假设K级指令流水线总延时是1纳秒，则有
 - 处理器时钟周期是每级延时 = 1/K 纳秒
 - 处理器主频 = K GHz
 - 指令流水线同时执行K条指令，平均每个时钟周期执行完毕一条指令
 - 处理器峰值速度：K GIPS



4. Postel's robustness principle 宽进严出原理

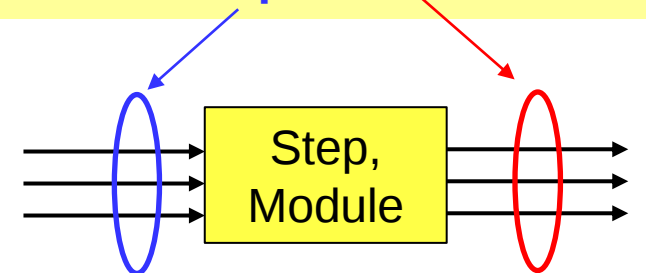
- Originally proposed by Jon Postel for the Internet
 - Has become a systems principle
- When design, implement, and use a system, for every step, every module
 - Be tolerant of inputs and strict on outputs (宽进严出)
 - Be tolerant of inputs
 - System should still work when inputs deviate somewhat from "correct" values
 - Be strict on outputs
 - System should generate only "correct" outputs, not deviating from "correct" values
- Implication
 - Accumulation of noises, errors, drifts, and distortions can be alleviated
噪音、误差、漂移、失真不会积累

《荀子•正名篇》
以仁心说，以学心听，
以公心辨。
荀子，前313~前238

TCP implementations should follow a general principle of robustness: be conservative in what you do, be liberal in what you accept from others.

Jon Postel, 1980

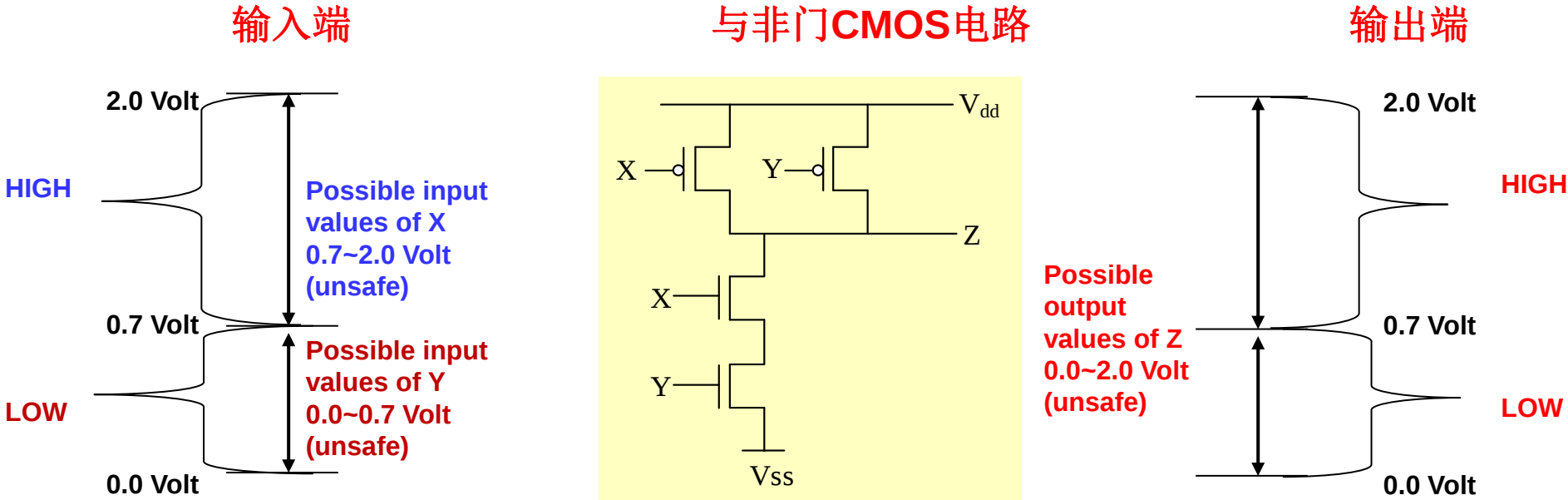
Be **strict in outputs**, and be **tolerant of inputs**



与非门电路设计:

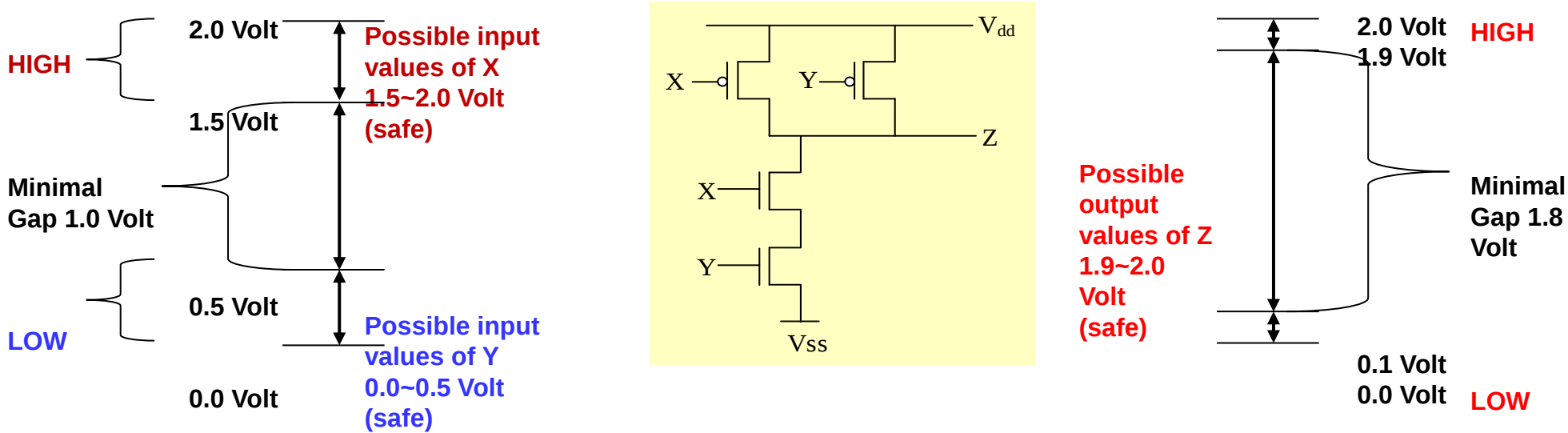
糟糕设计

- 宽进宽出
- 高低无间隙



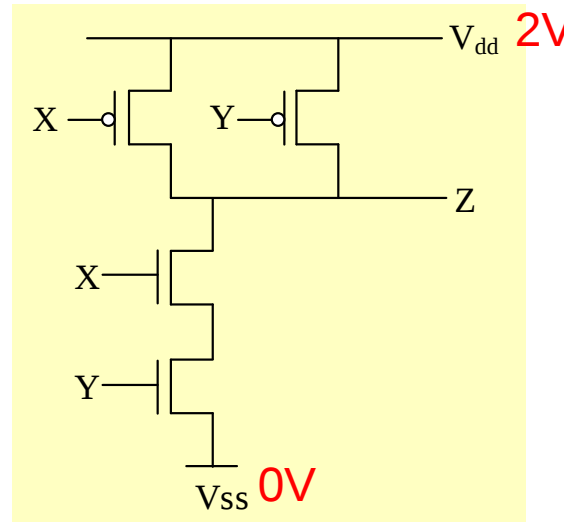
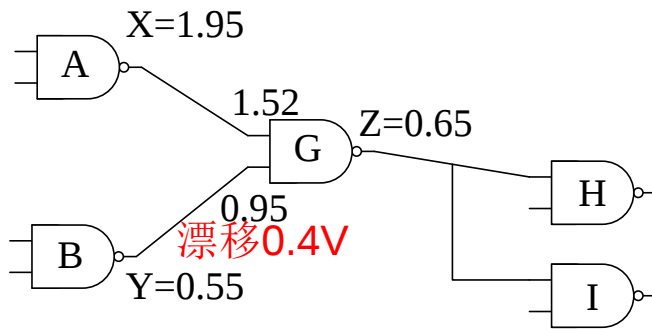
更佳设计

- 宽进严出
- 高低大间隙



Naïve Design

- Consider gate G in the circuit of 5 NAND gates
 - It receives inputs from A, B, and outputs to H, I
 - All NAND gate have the same behavior and been implemented by a CMOS circuit
 - Naïve Design of the CMOS circuit without following Postel's robustness principle
违反波斯特鲁棒原理的糟糕设计
 - There is **no gap** near the threshold voltage $V_{th} = 0.7$ Volt
 - When $A=HIGH=1.95$ and $B=LOW=0.55$ Volt, Z should be $HIGH > 0.7$ Volt
 - However, after B drifts $+0.4$ Volt to reach 0.95 Volt, Z becomes LOW, an **error**

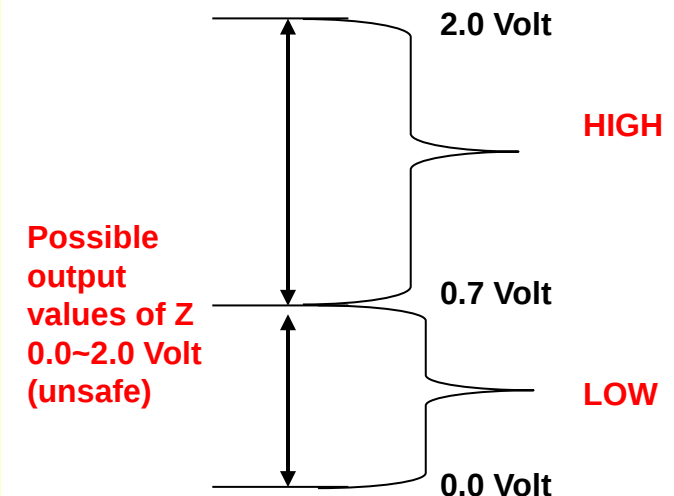
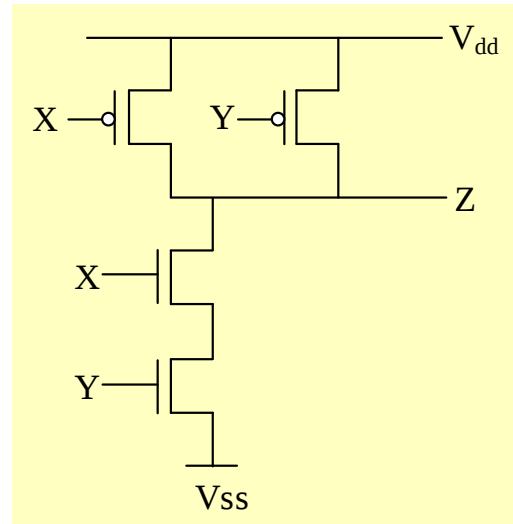
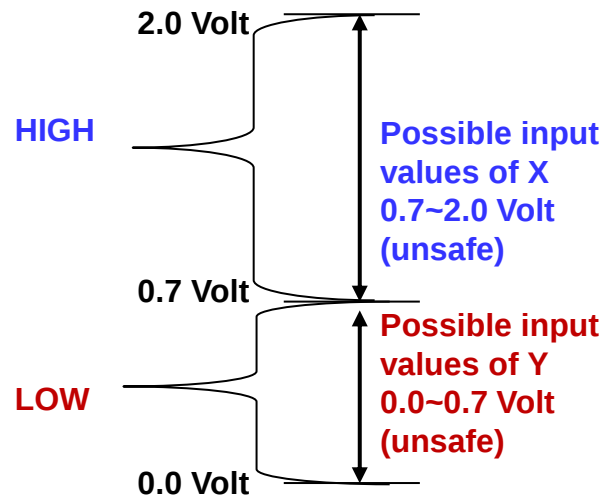


$V_{dd} = 2$ Volt 高电压
 $V_{ss} = 0$ Volt 低电压
 $V_{th} = 0.7$ Volt 阈值电压

Naïve Design
Logic 1: > 0.7 Volt
Logic 0: < 0.7 Volt

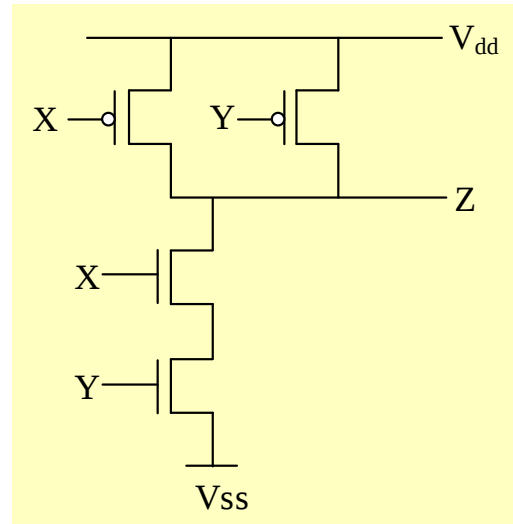
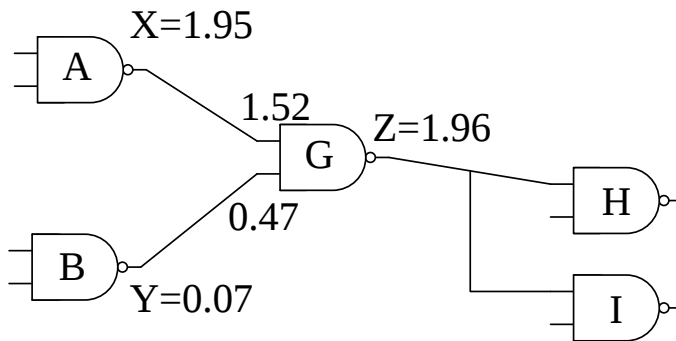
Summary of Naïve Design

- Assume **X=HIGH** and **Y=LOW**. Then **Z should be HIGH**
 - But, could easily get the wrong result of $Z = \text{LOW}$
- Why?
- Treat inputs and outputs equally, and in a bad way 宽进宽出，且不合理余量
 - Both the input side and the output side
 - have **0 minimal gap** between HIGH and LOW
 - have **unsafe margins** of 0.7 Volt for LOW and 1.3 Volt for HIGH



A better design 遵循波斯特鲁棒原理的更佳设计

- The better design following Postel's robustness principle
 - A minimal **gap of 1.0 volt at the input side**
 - A minimal **gap of 1.8 volt at the output side**
 - Note that the output of B cannot be 0.55 Volt. It has to be < 0.1 Volt
 - Let $B=LOW=0.07 < 0.1$ Volt. Even after a drifting value of $+0.4$ Volt, G still sees a LOW value, since $B=0.47$ Volt.
 - Thus, Z is HIGH with $Z > 1.9$ Volt



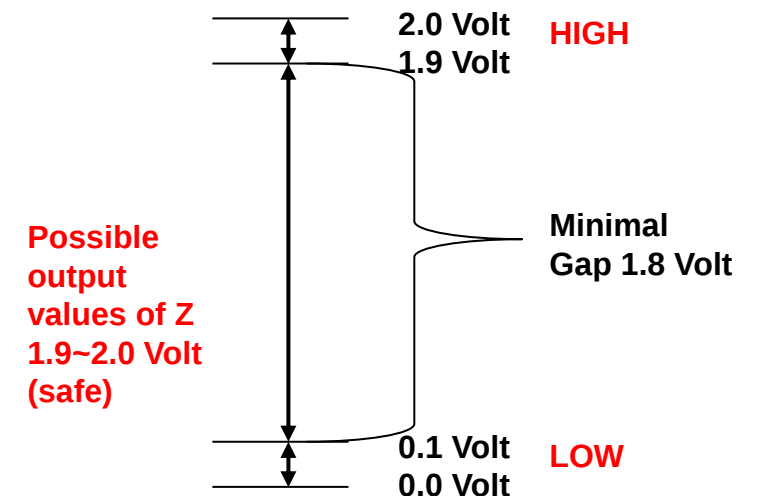
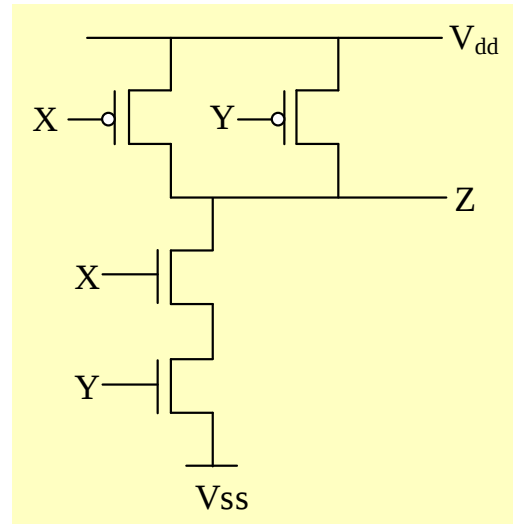
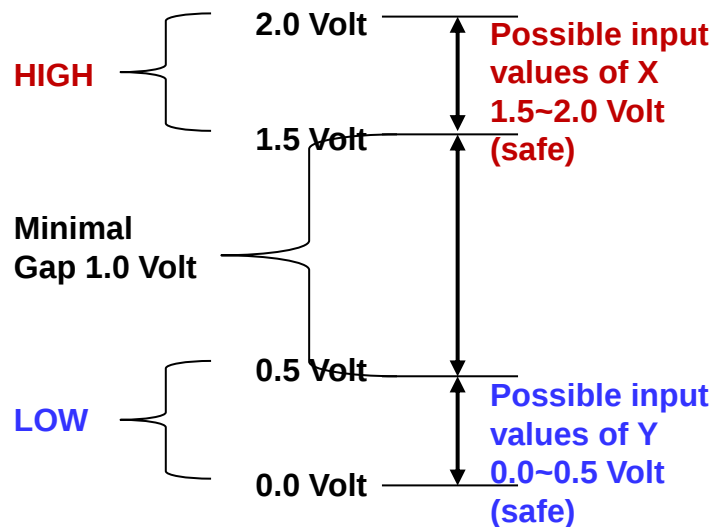
Better Design

For Input Voltages
Logic 1: > 1.5 Volt
Logic 0: < 0.5 Volt

For Output Voltages
Logic 1: > 1.9 Volt
Logic 0: < 0.1 Volt

Summary of Better Design

- Assume **X=HIGH** and **Y=LOW**. Then **Z will be HIGH**
- **Tolerance on inputs** 宽进
 - Input to a gate has a 0.5 Volt safe margin and a minimal gap of 1 Volt
 - Naïve Design: 0.7 and 1.3 unsafe margins and 0 minimal gap
- **Strictness on outputs** 严出
 - Output from a gate has a 0.1 Volt safe margin and a minimal gap of 1.8 Volt
 - Naïve Design: 0.7 and 1.3 unsafe margins and 0 minimal gap



5. von Neumann's exhaustiveness principle

冯诺依曼穷尽原理

- Computer must be given instructions **in absolutely exhaustive detail** when automatically solving a problem
当自动解决问题时，必须给计算机指令，它们穷尽所有细节
- In the quote, two terms have specific meanings
 - *Operation* = Problem-solving Task
 - E.g., solving a non-linear partial differential equation
 - *Device* = Computer
 - An automatic computing system

The instructions which govern this *operation* must be given to the *device* in absolutely exhaustive detail. ...

Once these instructions are given to the device, it must be able to carry them out completely and without any need for further intelligent human intervention.

John von Neumann, 1945

von Neumann's exhaustiveness principle

- Computer must be given instructions in absolutely exhaustive detail when automatically solving a problem
- 1-minute quiz
 - Q: How to cover “absolutely exhaustive detail”? 怎么可能穷尽所有细节?
 - 可能有无穷多种细节，如何穷尽?
 - 使用前述**计算归纳法**
 - Identify first step
确定第一步
 - Execute single step
正确执行每一步（当前步骤）
应对异常
 - Identify and transition
to next step 确定并过渡到下一步

The instructions which govern this operation must be given to the device in absolutely exhaustive detail. ...

Once these instructions are given to the device, it must be able to carry them out completely and without any need for further intelligent human intervention.

John von Neumann, 1945

von Neumann's exhaustiveness principle

- Computer must be given instructions in absolutely exhaustive detail when automatically solving a problem
- 1-minute quiz
 - Q: How to achieve “in absolutely exhaustive detail”? List the types of instructions, and give an example for each type
 - A: Answers to more fundamental questions 必须考虑正常执行和异常执行
 - Where and what is the first instruction, when the computer power is turned on?
开机之后执行的**第一条指令**在哪里？是什么？
 - How to determine the next instruction to execute?
如何确定**下一条指令**？
 - What types of exceptions are there, to normal execution of programs?
如何保证**当前指令**正确执行？
没有正确执行，只有两种可能：（1）没有正确设计实现；（2）出现**异常**
有哪些异常类别？如何应对？

The first instruction to execute

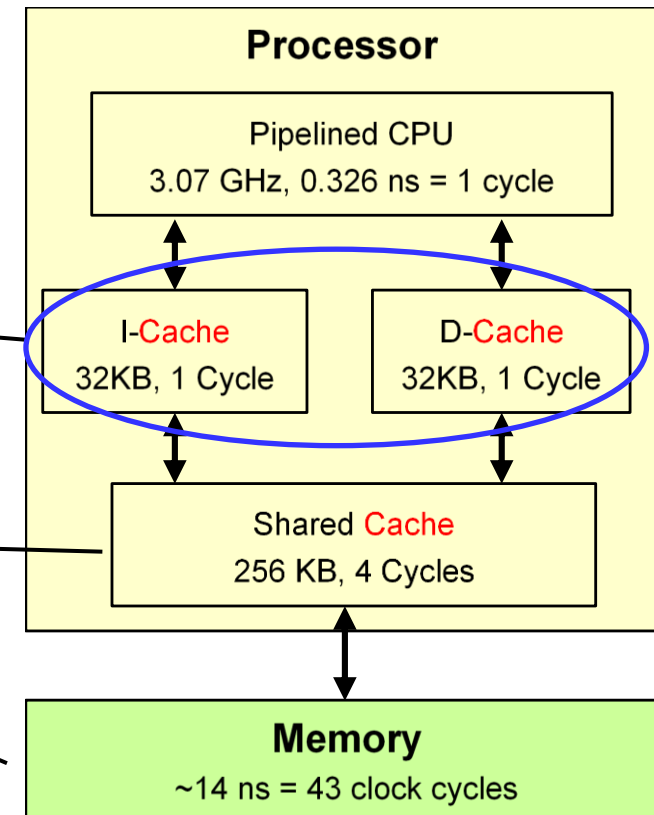
when the computer power turns on

开机后执行的第一条指令：在哪里？是什么？

- Example with an x86 processor **x86处理器例子**
 - Where: the first instruction to execute is at memory address 0xFFFFFFFF0
在哪里？处理器规定的地址空间的某个高位地址
 - What: a jump instruction, e.g., JUMP 000F0000 是什么
 - Address 000F0000 contains the entry instruction for the BIOS code
跳转指令：跳转到BIOS（最底层系统软件）的入口地址
- Why? 什么道理？
 - Computer starts by executing the BIOS firmware code
 - To initialize the computer and to load the operating system
计算机开机后先执行固件，做初始化工作（如自检），然后载入系统软件
 - Using a jump instruction upfront increases flexibility
跳转指令增加灵活性
 - E.g., if we want the computer to start by executing another firmware code BIOS-2 at entry address 000FA000, then change
 - Address 0xFFFFFFFF0 to hold JUMP 000FA000

Three ways to determine 确定下一条指令的方法1 the **next instruction** to execute

- The earliest method is **linear sequencing** in Harvard Mark I computer, the *Automatic Sequence Controlled Calculator*
 - Instructions are linearly sequenced
下一条指令紧跟当前指令
 - There is no jump. Next instruction is located right after current instruction on the instruction tape 指令纸带
 - Storing data and code separately
(This is called **Harvard architecture**)
哈佛体系结构
 - Still widely used in the cache units of modern computers. A processor has separate instruction cache and data cache
 - In contrast, the **Princeton architecture**
普林斯顿体系结构
uses a single cache or memory to store both data and instructions
- Modern computers use both



Three ways to determine the **next instruction** to execute

确定下一条指令的方法2、3

- The **ENIAC method**

ENIAC方法

- Every instruction holds the address of the next instruction

当前指令指明下一条指令的地址

万维网页使用类似思路：当前网页包含下一网页地址

- Used by the revised version of the ENIAC computer

Opcode and operands of current instruction	Address of next instruction
--	-----------------------------

- Modern computers mostly use the **PC mechanism**: the address of the next instruction to execute is stored in the **program counter (PC)**

当代计算机采用“程序计数器机制”

程序计数器（**PC**）存放下一条指令的地址

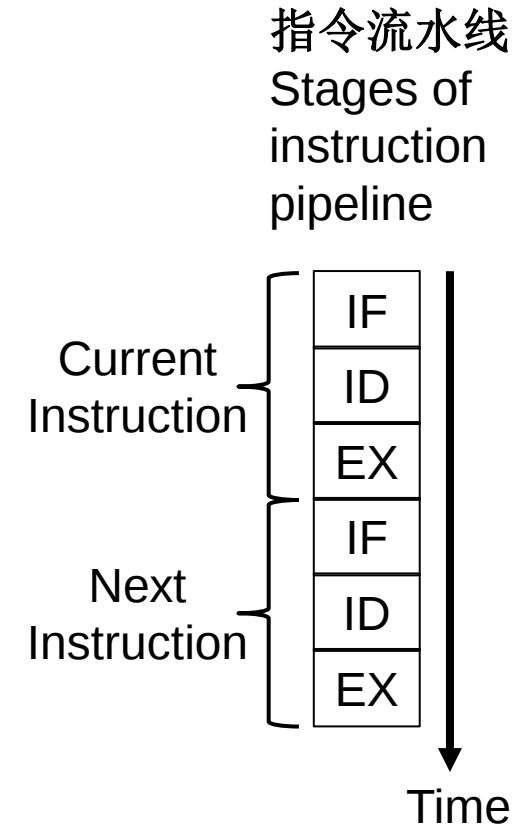
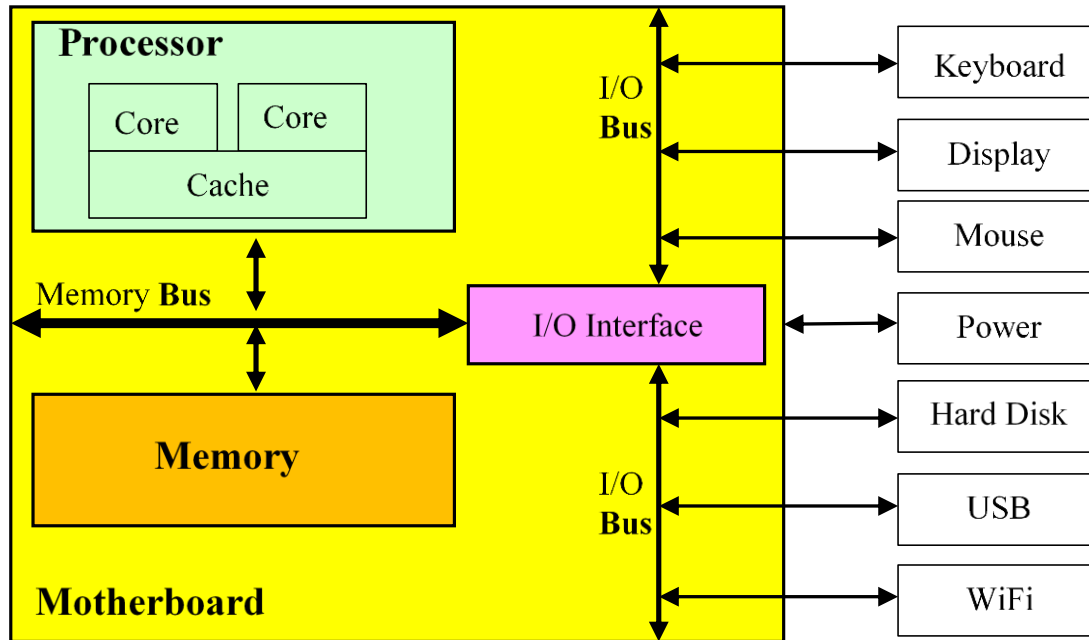
Deal with **exceptions** to normal execution

应对异常

- 同学们已经体验过了Go语言编程中的异常
 - 读文件可能出错
- We have seen exceptions in programming, e.g., in the Text Hider project, the statement
 - `p, _ := ioutil.ReadFile("./Autumn.bmp")` 例如，文件不存在should really be
 - ```
p, error := ioutil.ReadFile("./Autumn.bmp")
if error != nil {
 ...// put exception-handling code here 出错了，执行异常处理代码
}
... // no error; continue normal execution 无错，继续正常执行
```

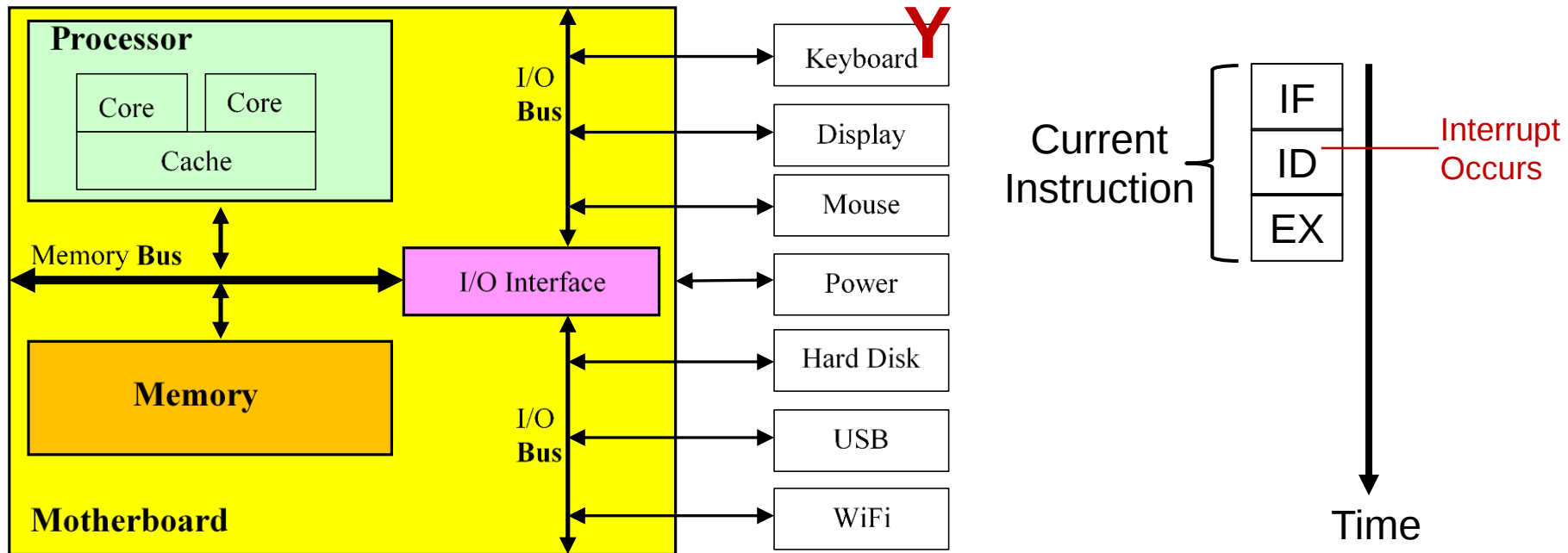
# Three types of exceptions are supported by computer hardware 三种异常

- In normal execution (without exception), the current instruction finishes and continue to execute the next instruction  
正常情况：执行完当前指令，继续执行下一条指令
- 异常情况：（1）不执行完当前指令；（2）不执行下一条指令；
  - Interrupt 中断
  - Hardware error 硬件出错
  - Machine check 保底异常



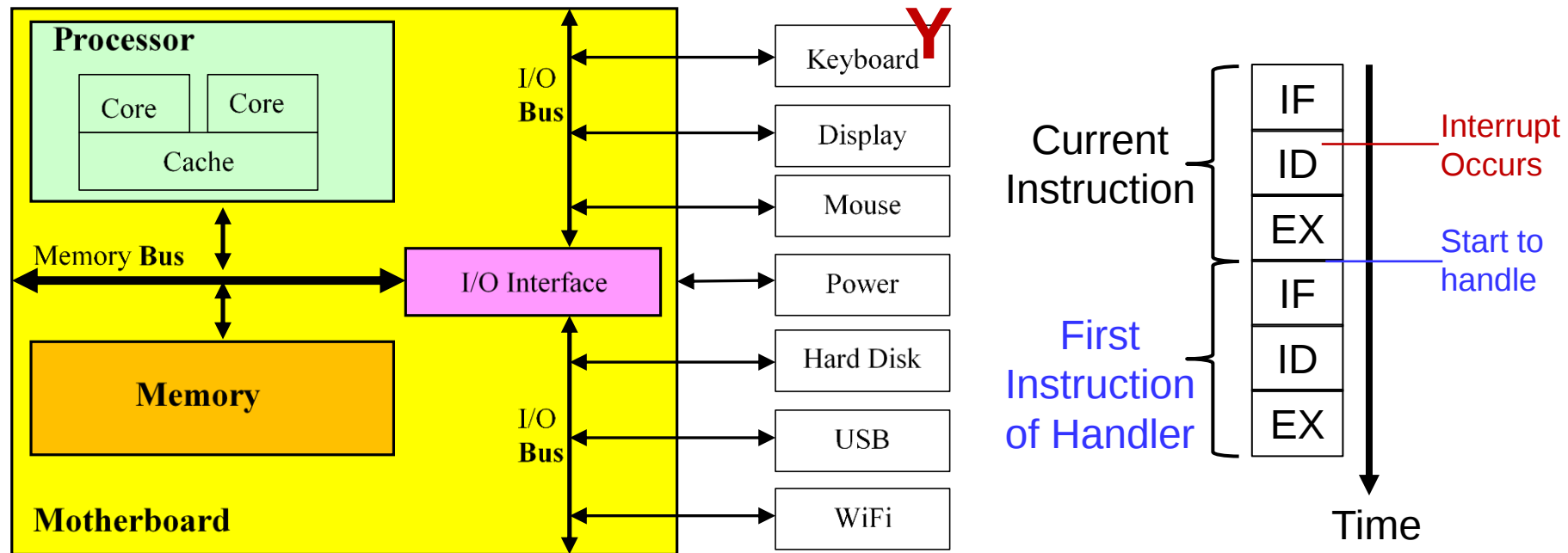
# Interrupt handling 中断处理

- When an **interrupt** occurs, e.g.,
  - When the user punches key 'Y' on the keyboard 用户敲了'Y'键 while the processor is executing the instruction decode stage
- What should the processor do?
  - Should it immediately take an exception-handling action?
  - Should it finish the current instruction first?



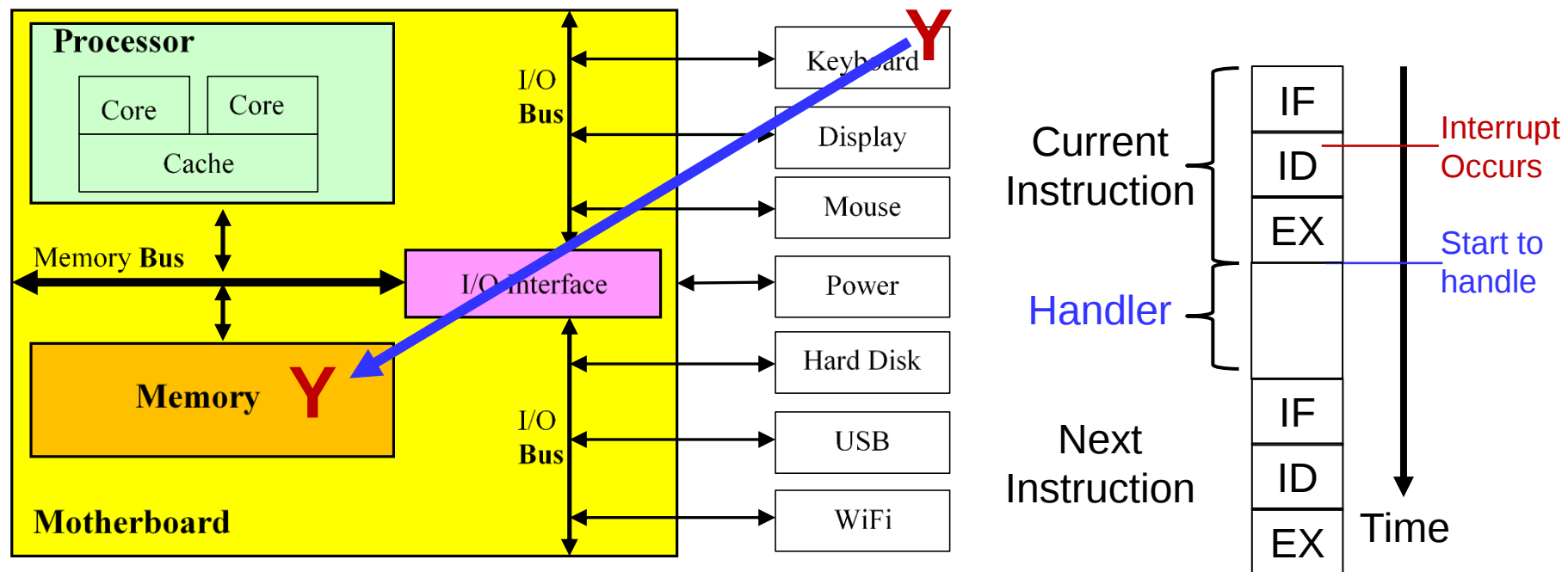
# Interrupt handling

- 继续执行完毕当前指令，然后跳转到中断处理程序的入口
- The processor finishes the current instruction and jumps to an interrupt handling subprogram to handle the interrupt
  - 中断处理程序称为 interrupt **handler**



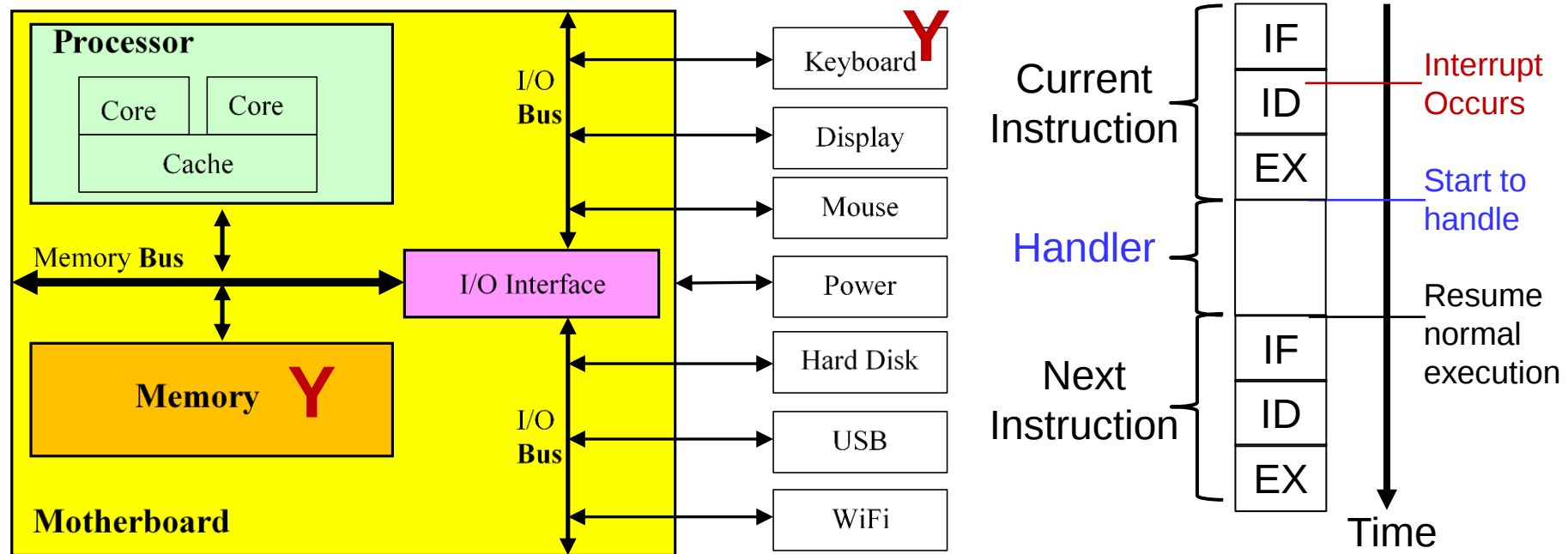
# Interrupt handling

- The processor finishes the current instruction and jumps to an interrupt handling subprogram to handle the interrupt
  - such as **copying the punched key value to memory**  
执行中断处理程序，包括将敲入的键值'Y'拷贝到内存



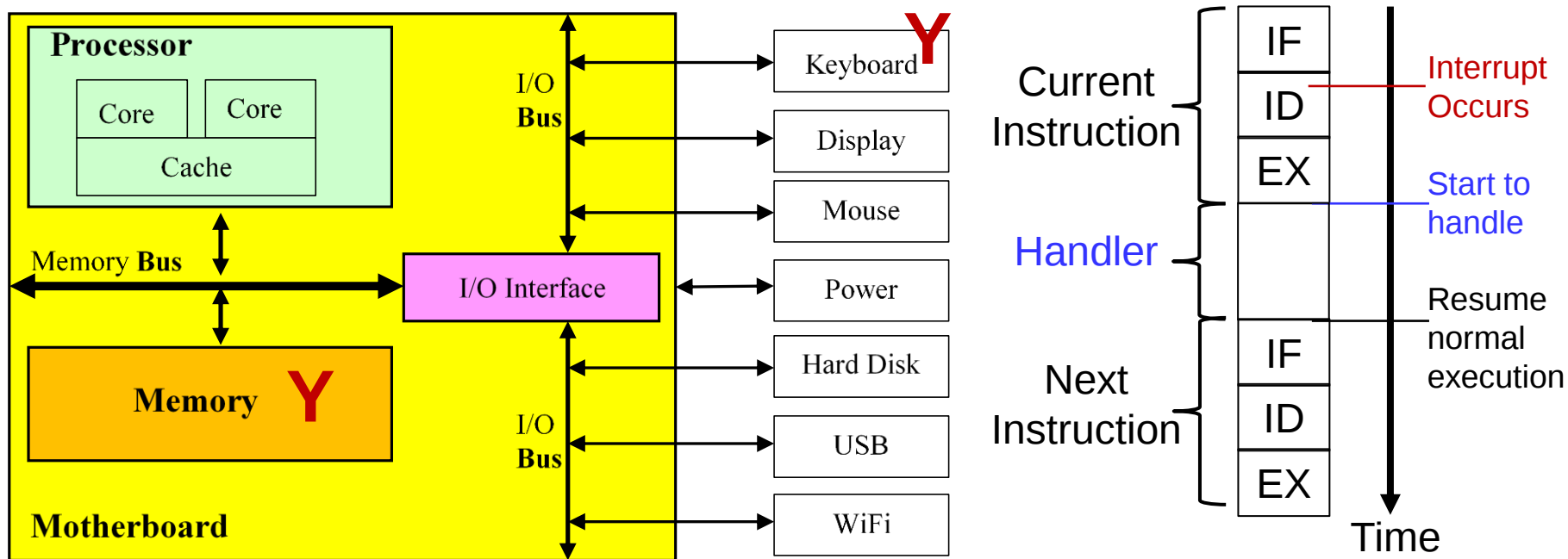
# Interrupt handling

- When an **interrupt** occurs, the processor finishes the current instruction and jumps to an interrupt handling subprogram to handle the interrupt
  - such as **copying the punched key value to memory**
- Then, the processor resumes normal execution
  - by executing the original next instruction  
退出中断处理程序，恢复正常执行原来程序的下一条指令



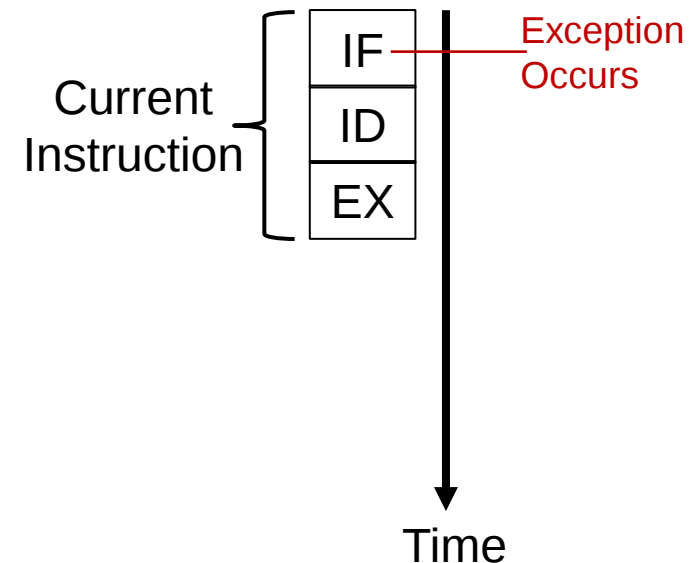
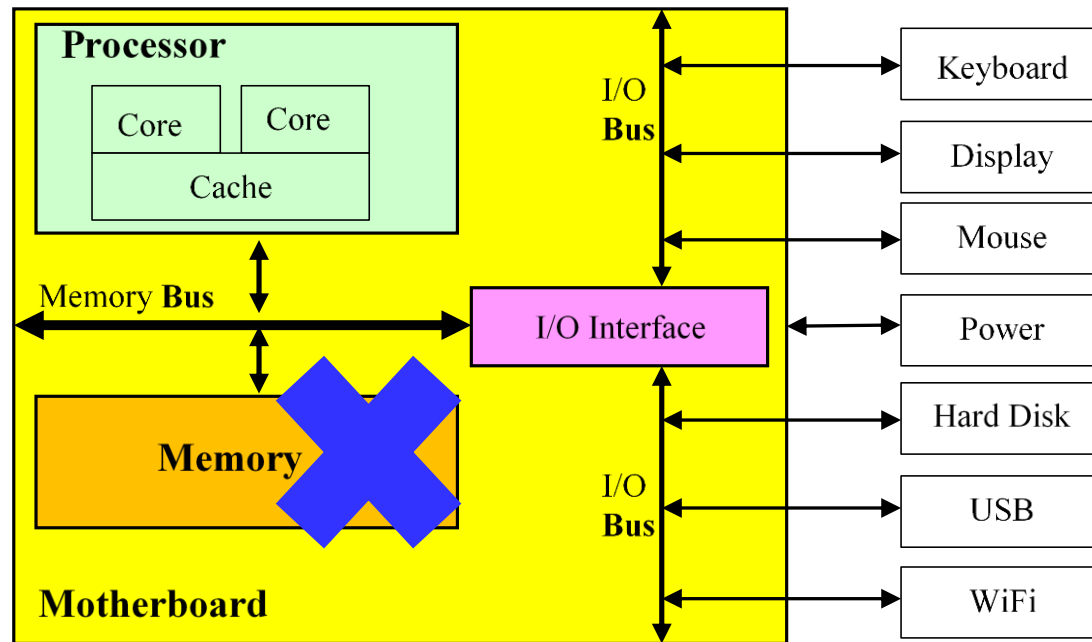
# Interrupt handling

- When an **interrupt** occurs, the processor finishes the current instruction and jumps to an interrupt handling subprogram to handle the interrupt
  - such as **copying the punched key value to memory**
- Then, the processor resumes executing the next instruction
  - Q: how does the processor know the address of the next instruction?
  - A: need to **save context** before executing handler  
进入中断处理程序前，必须**保存上下文**，知道返回后该执行哪条指令



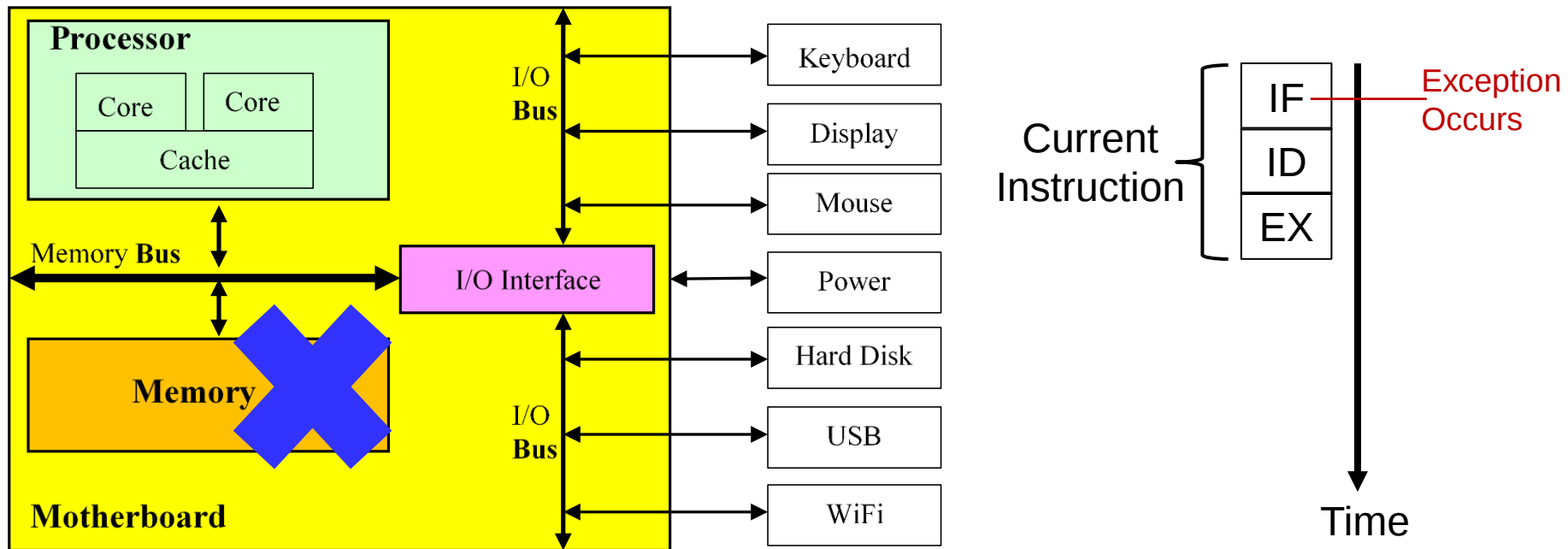
# Hardware error handling 硬件出错

- When a hardware error occurs, e.g.,
  - When the memory becomes faulty and generates a hardware error exception 例  
如，内存条坏了
- What should the processor do?
  - Should it immediately take an exception-handling action?
  - Should it finish the current instruction first?



# Hardware error

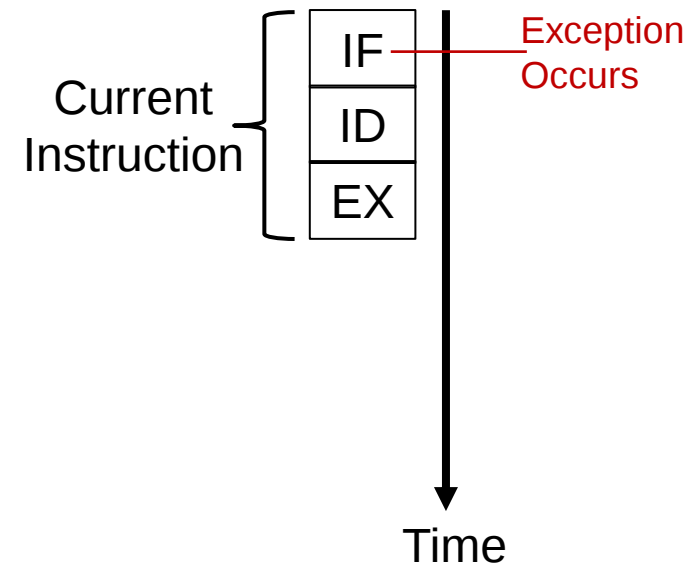
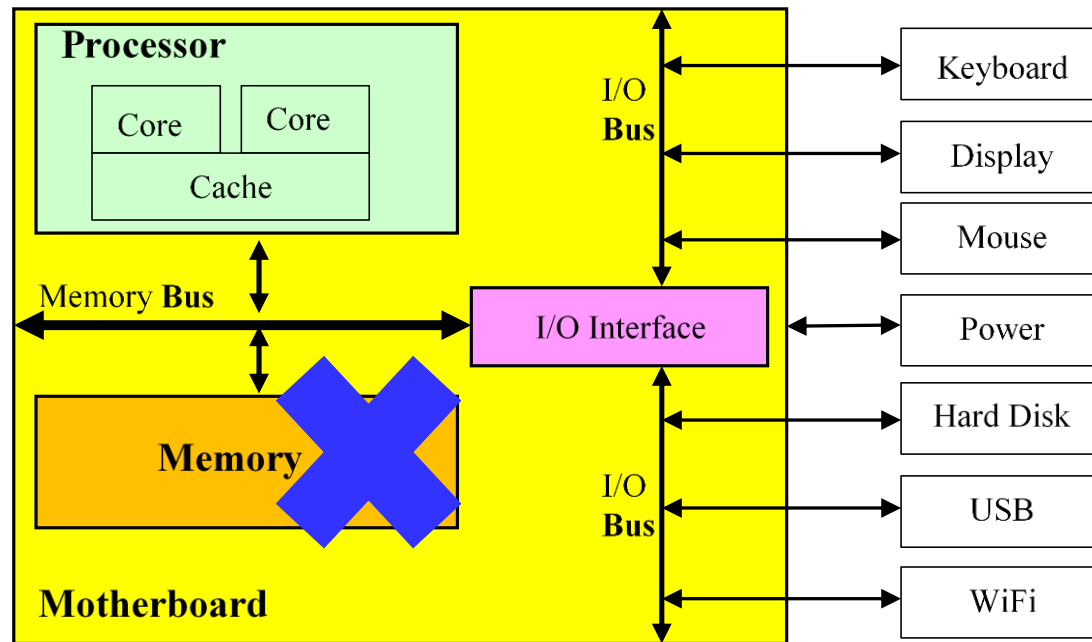
- When the memory becomes faulty and generates a hardware error exception  
内存条坏了
  - Should the processor finish the current instruction first?  
还能够先完成当前指令再“中断”吗?
  - No, because the IF stage cannot be finished 不行! 指令都取不回来
    - The instruction cannot be fetched from memory 完不成取指 (IF) 操作



# Hardware error

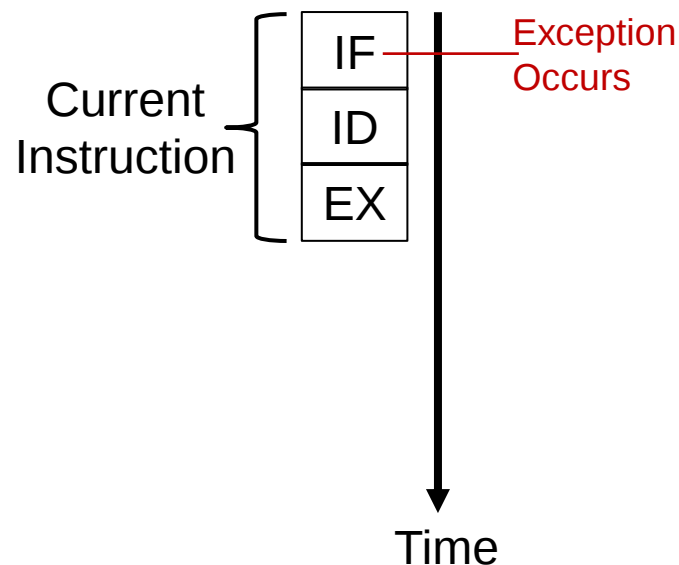
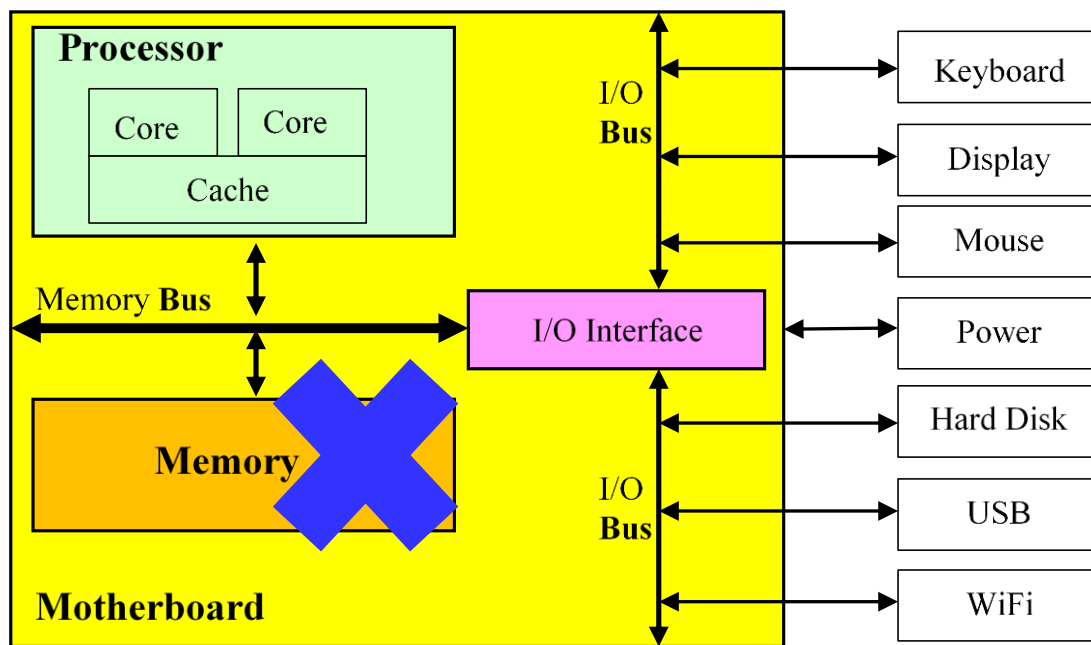
- When the memory becomes faulty and generates a hardware error exception
  - Should the processor immediately take an exception-handling action?
  - Yes, it executes an exception-handling sequence of steps without depending on the memory

立即执行异常处理程序，无需访问内存



# Machine check 保底异常

- This is the "all other" exception, for exhaustiveness
    - Typically, an unrecoverable hardware error
  - Example
    - While executing an exception-handling sequence of steps for the memory fault, the sequence experiences another error
    - The system generates minimal diagnostic information and crashes
- 产生最基本的诊断信息，宕机



## 6. Amdahl's law

- Previous 3 principles regard correctness (seamless transition)
- Amdahl's law focuses on performance (smooth transition)
- 1-minute quiz
  - A student writes a program `sort.go` to read an 8-GB file of 64-bit integers, sort the integers, and write the sorted result into another file on his laptop computer. Suppose the total execution time is  $T$ , where  $0.8 \cdot T$  is spent on I/O operations.
    - Q1: What is the problem size  $N$ , i.e., the number of integers?
    - A1: (a) 8 (b) 64 (c) 1024 (d)  $64 \cdot 1024 \cdot 1024$  (e)  $1024 \cdot 1024 \cdot 1024$
    - Q2: The student upgrades his laptop with a new wonder processor that is 100 times as fast as the old processor. How much time (approximately) is needed to execute `sort.go` on the same 8-GB file?
    - A1: (a)  $T/100$  (b)  $T/5$  (c)  $0.1 \cdot T$  (d)  $0.8 \cdot T$

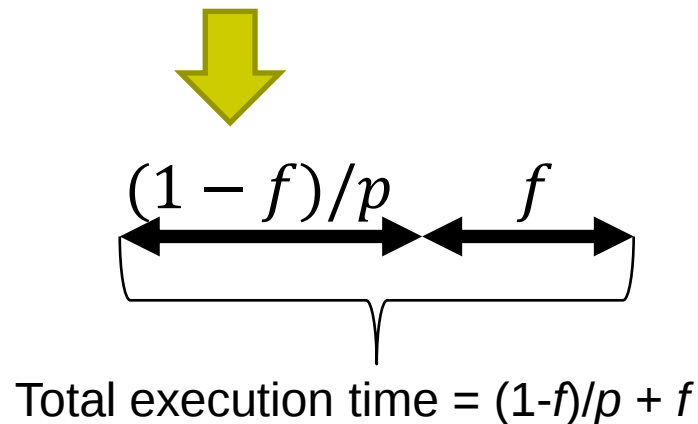
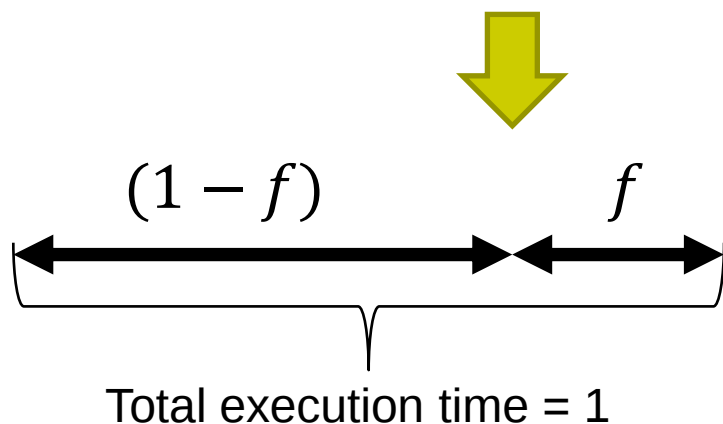
# Amdahl's law

- 1-minute quiz

- A student writes a program sort.go to read an 8-GB file of 64-bit integers, sort the integers, and write the sorted result into another file on his laptop computer. Suppose the total execution time is  $T$ , where  $0.8 \cdot T$  is spent on file I/O operations.
- Q1: What is the problem size  $N$ , i.e., the number of integers?
- A1: (a) 8 (b) 64 (c) 1024 (d)  $64 \cdot 1024 \cdot 1024$  (e)  $1024 \cdot 1024 \cdot 1024$
- Q2: The student upgrades his laptop with a new wonder processor that is 100 times as fast as the old processor. How much time (approximately) is needed to execute sort.go on the same 8-GB file?
- A1: (a)  $T/100$  (b)  $T/5$  (c)  $0.1 \cdot T$  (d)  $0.8 \cdot T$ 
  - The processing time is about  $0.2 \cdot T/100$ , but the I/O time stays the same. Thus, the total time is about  $0.2 \cdot T/100 + 0.8 \cdot T = 0.802 \cdot T$
  - The speedup is  $T / 0.802T \approx 1.247$ , only 24.7% faster

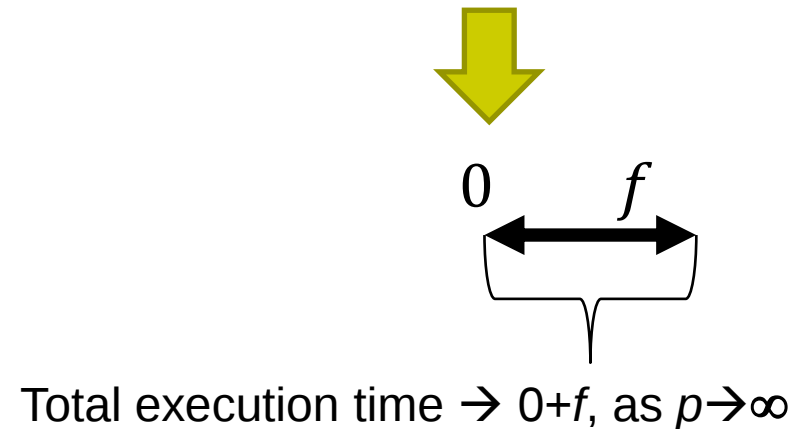
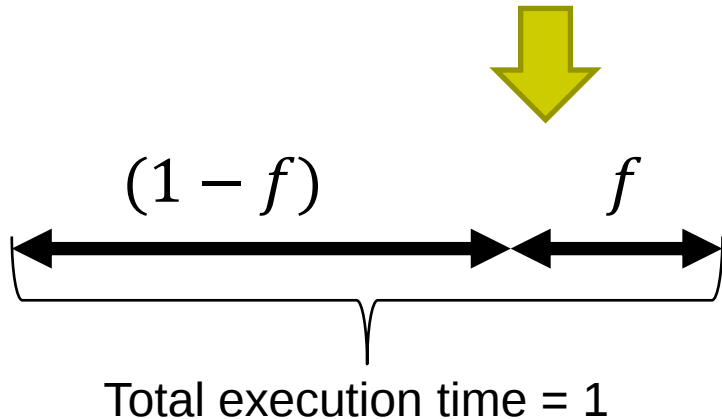
# Amdahl's law 阿姆达尔定律

- Suppose a system's execution time is broken into two portions  $(1 - f)$  and  $f$ , such that  $(1 - f) > f$  系统执行时间1划分成两部分 $(1 - f)$ ,  $f$
- Amdahl's law: Enhancement on the  $(1 - f)$  portion can lead to a speedup no more than  $1/f$  改进系统的一部分后，系统**加速比**不会超过未改进部分执行时间的倒数
  - Speedup approaches but never exceeds  $1/f$
  - **Speedup** = (time before enhancement) / (time after enhancement)  
**加速比** = 改进前的执行时间 / 改进后的执行时间



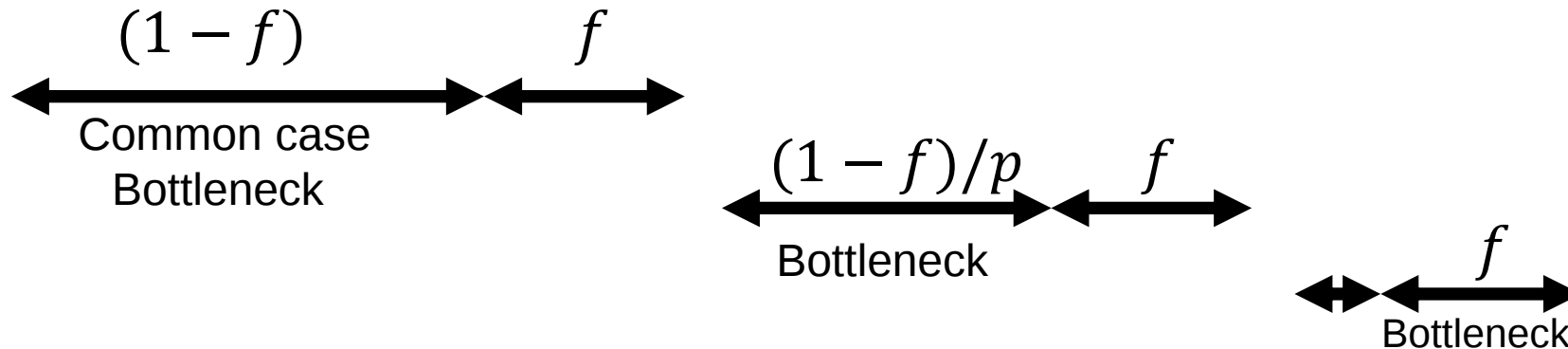
# Amdahl's law

- After enhancing a portion of a system, the speedup obtained is upper bounded by the reciprocal of the other portion's time, i.e.,  $1/f$ 
  - **Speedup** = (time before enhancement) / (time after enhancement)  $\approx 1/f$  at most



# Implications of Amdahl's law

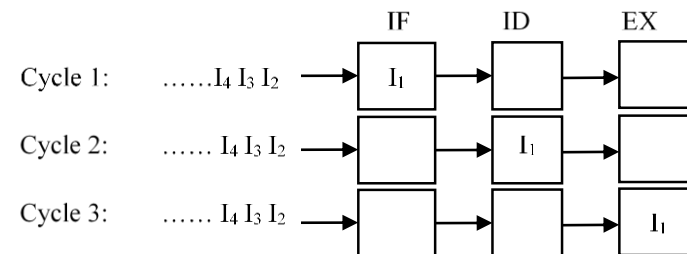
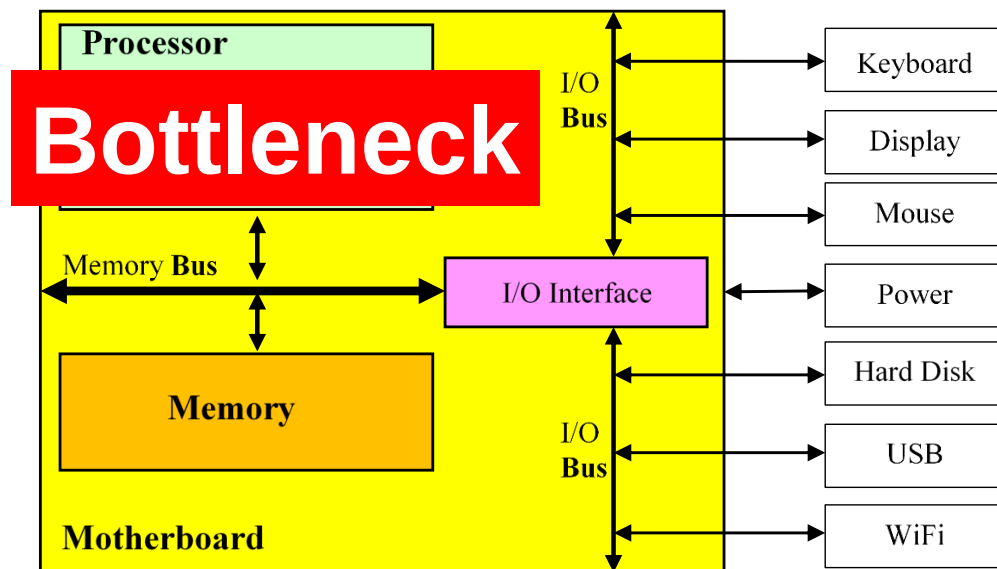
- Amdahl's law offers two advices for system design
  - *Optimize the common case*. System enhancement, or system optimization, should focus on the common case, also known as the bottleneck, i.e., the most time-consuming portion  
改进瓶颈
  - *Chase the bottleneck*. When the system bottleneck changes, so does our optimization target  
追逐瓶颈



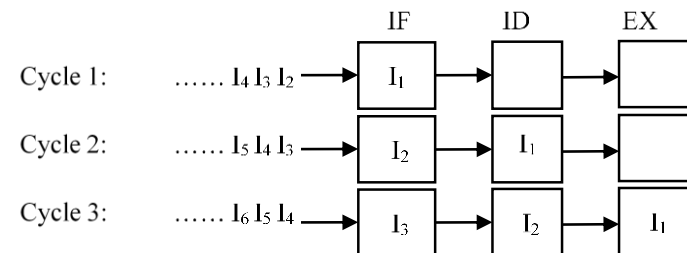
- Three techniques to utilize Amdahl's law
  - Pipelining, caching, parallel computing

## 6.1 Pipelining: multiple instructions overlap

- Optimize the bottleneck of the CPU's instruction pipeline
  - Key technique: overlapping pipeline stages with multiple instructions
    - Using about the same amount of resource, plus some overhead
- Assuming 1-GHz clock cycle, the average performances are
  - Without overlapping: executing an instruction needs 3 cycles and 3 ns
  - With overlapping: executing an instruction needs 1 cycle and 1 ns



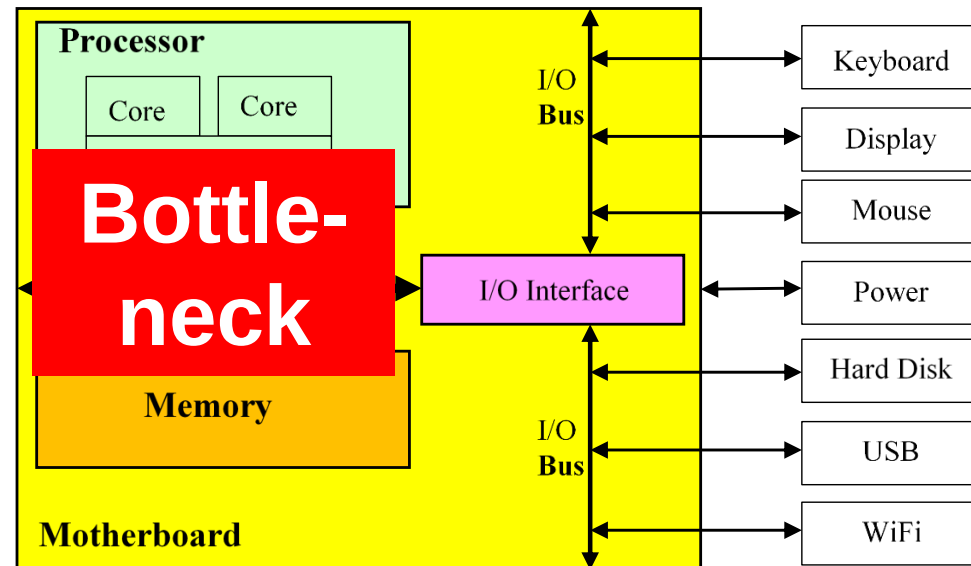
(a) No overlapping of pipeline stages



(b) Overlapping of pipeline stages

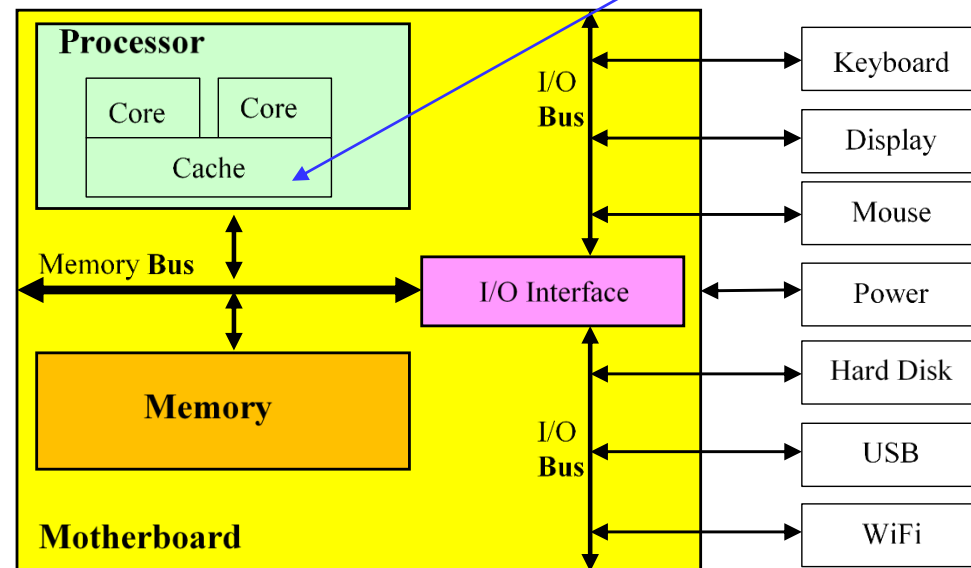
## 6.2 Caching: use a small but faster buffer

- Optimize the von Neumann bottleneck
  - Memory is too slow to feed data to CPU
  - On the other hand, programs have spatial and temporal **localities**
  - Key technique: caching, i.e., using a small but faster buffer



# Caching: use a small but faster buffer

- Optimize the von Neumann bottleneck
  - Memory is too slow to feed data to CPU
  - On the other hand, programs have spatial and temporal localities
  - Key technique: caching, i.e., using a small but faster **buffer**
    - Without having to change the instruction set



- Design and back-of-envelop performance analysis

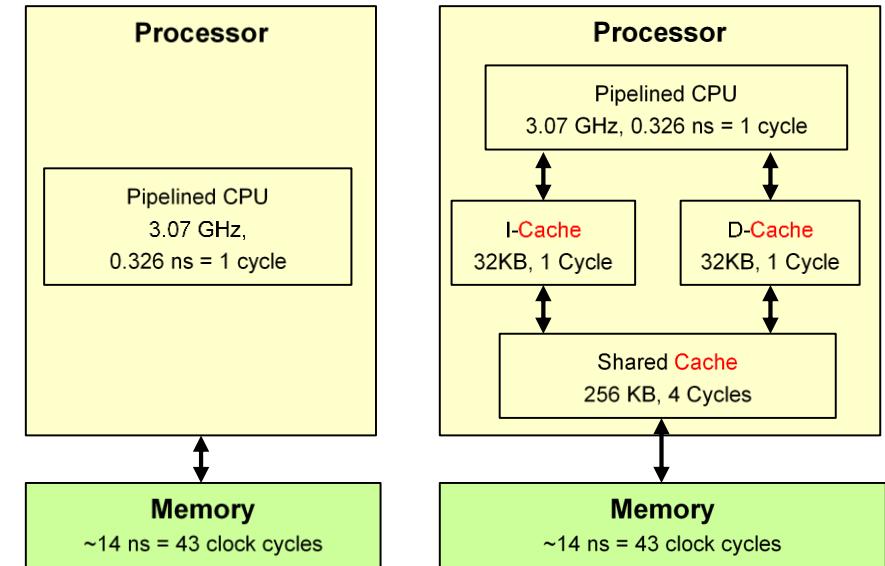
# \*\*\*Caching using the Fibonacci Computer

- Two-layer caching
  - Layer 1: separate instruction and data caches
  - Layer 2: shared cache for instruction and data
- Assume 92 iterations of the loop code in red are executed

Clock cycles of instructions without caching

| Instruction type | Times of memory accesses | Clock cycles needed             |
|------------------|--------------------------|---------------------------------|
| MOV 0, R1        | 1                        | $1 \cdot 43 + 1 \rightarrow 43$ |
| MOV R1, M[...]   | 2                        | $2 \cdot 43 + 1 \rightarrow 86$ |
| ADD M[...], R1   | 2                        | $2 \cdot 43 + 1 \rightarrow 86$ |
| INC R2           | 1                        | $1 \cdot 43 + 1 \rightarrow 43$ |
| CMP 51, R2       | 1                        | $1 \cdot 43 + 1 \rightarrow 43$ |
| JL Loop          | 1                        | $1 \cdot 43 + 1 \rightarrow 43$ |

Numbers in **blue** are canceled out due to pipeline overlapping. A simpler analysis does not consider such optimizations, and calculate the cycles for “MOV 0, R1” to be  $1 \cdot 43 + 1 = 44$ . This simplification leads to similar performance analysis results.



|                       | No Caching | Caching |
|-----------------------|------------|---------|
| MOV 0, R1             | 43         |         |
| MOV R1, M[R0]         | 86         |         |
| MOV 1, R1             | 43         |         |
| MOV R1, M[R0+8]       | 86         |         |
| MOV 2, R2             | 43         |         |
| Loop: MOV 0, R1       | 43         | 1       |
| ADD M[R0+R2*8-16], R1 | 86         | 1       |
| ADD M[R0+R2*8-8], R1  | 86         | 2       |
| MOV R1, M[R0+R2*8-0]  | 86         | 2       |
| INC R2                | 43         | 1       |
| CMP 51, R2            | 43         | 2       |
| JL Loop               | 43         | 3       |

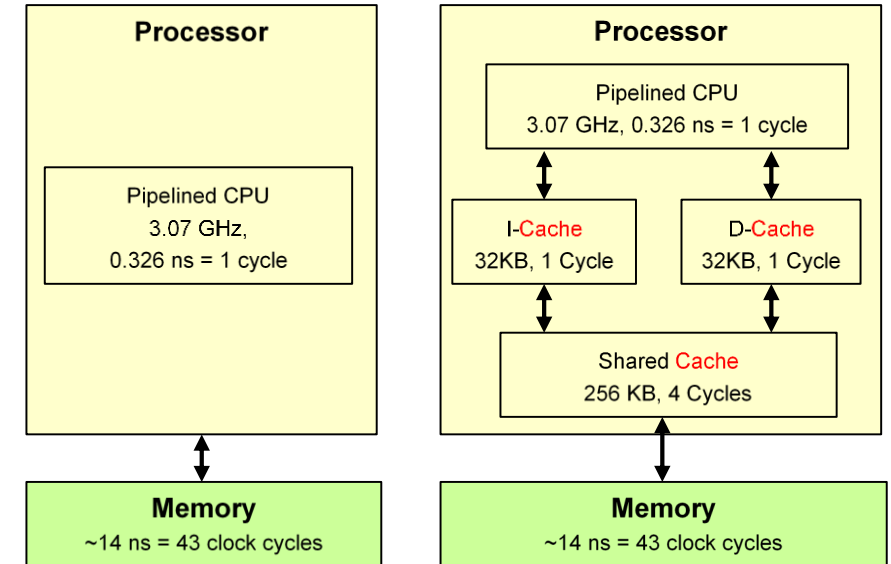
Assume all internal operations together take 1 cycle. Every instruction execution needs to access memory at least once to fetch instruction. Some instructions need two accesses to also fetch data.

# \*\*\*When code and data are stored in level-1 caches

- Instruction Fetch needs only 1 cycle
  - This is why 1<sup>st</sup> MOV needs 1 cycle
- Instruction Fetch and Operand Fetch can be done simultaneously, thanks to Harvard architecture
  - This is why 1<sup>st</sup> ADD needs 1 cycle
- Data and control **dependencies** may cause pipeline to stall (wait)
  - This is why 2<sup>nd</sup> ADD needs 2 cycles and JL needs 3 cycles

## Clock cycles of instructions **with caching**

| Instruction type | Times of memory accesses | Clock cycles needed  |
|------------------|--------------------------|----------------------|
| MOV 0, R1        | 1                        | 1*1 <b>+1</b> → 1    |
| MOV R1, M[...]   | 2                        | 1*1 <b>+1</b> → 1    |
| ADD M[...], R1   | 2                        | 1*1 <b>+1</b> → 1    |
| INC R2           | 1                        | 1*1 <b>+1</b> → 1    |
| CMP 51, R2       | 1                        | 1*1 <b>+1 +1</b> → 2 |
| JL Loop          | 1                        | 1*1 <b>+1 +2</b> → 3 |



|                       | No Caching | Caching |
|-----------------------|------------|---------|
| MOV 0, R1             | 43         |         |
| MOV R1, M[R0]         | 86         |         |
| MOV 1, R1             | 43         |         |
| MOV R1, M[R0+8]       | 86         |         |
| MOV 2, R2             | 43         |         |
| Loop: MOV 0, R1       | 43         | 1       |
| ADD M[R0+R2*8-16], R1 | 86         | 1       |
| ADD M[R0+R2*8-8], R1  | 86         | 2       |
| MOV R1, M[R0+R2*8-0]  | 86         | 2       |
| INC R2                | 43         | 1       |
| CMP 51, R2            | 43         | 2       |
| JL Loop               | 43         | 3       |

Assume all internal operations together take 1 cycle.  
 Every instruction execution needs to access memory at least once to fetch instruction. Some instructions need two accesses to also fetch data.

# Simplified performance analysis

- Simplify by consider a single iteration of loop

- Without caching

- Total time =  $4 \times 43 + 3 \times 86$   
= 430 clock cycles  
=  $430 \times 0.326 = 140$  ns

|                       | No Caching | Caching |
|-----------------------|------------|---------|
| Loop: MOV 0, R1       | 43         | 1       |
| ADD M[R0+R2*8-16], R1 | 86         | 1       |
| ADD M[R0+R2*8-8], R1  | 86         | 2       |
| MOV R1, M[R0+R2*8-0]  | 86         | 2       |
| INC R2                | 43         | 1       |
| CMP 51, R2            | 43         | 2       |
| JL Loop               | 43         | 3       |

- With caching

- Total time =  $1 \times 3 + 2 \times 3 + 3 \times 1$   
= 12 clock cycles  
=  $12 \times 0.326 = 3.91$  ns

- Caching brings about significant speedup

- **Speedup =  $140$  ns /  $3.91$  ns = 35.8, or 34.8 times faster**

# Performance metrics of the 3.07-GHz FC

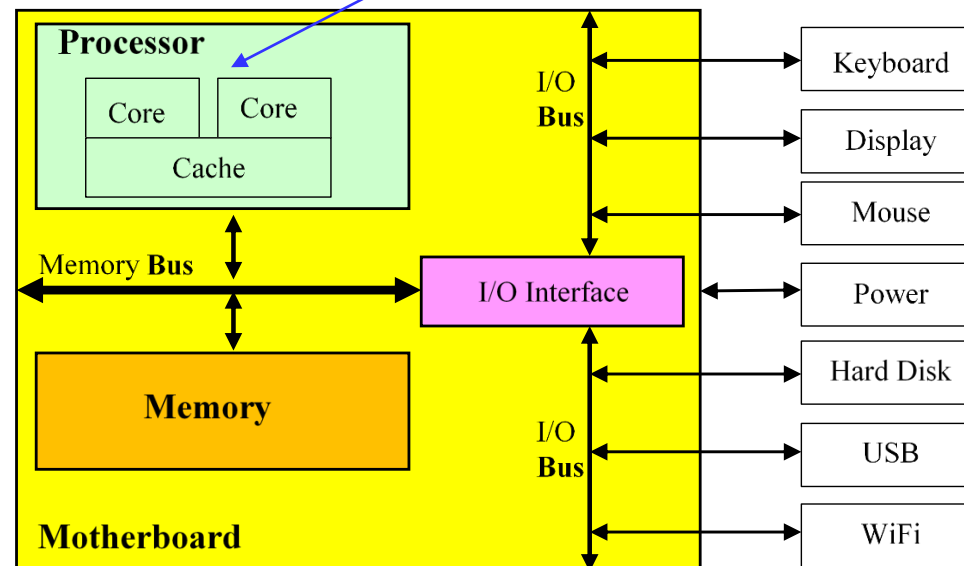
- The **peak speed** of the Fibonacci Computer is the maximal speed possible
  - Peak speed = 1 instruction per cycle = 3.07 GIPS
- The **sustained speed** of the Fibonacci Computer is the real speed achieved when executing the loop application code
  - Sustained speed =  $7/140 = 0.05$  GIPS
    - Each iteration takes 140 ns to execute 7 instructions
  - **Efficiency** = sustained speed / peak speed =  $0.05 / 3.07 = 1.63\%$

# Performance metrics of the 3.07-GHz FC

- The **peak speed** of the Fibonacci Computer is the maximal speed possible
  - Peak speed = 1 instruction per cycle = 3.07 GIPS
- The **sustained speed** of the Fibonacci Computer is the achieved speed when executing the loop application code
  - Sustained speed =  $7/140 = 0.05$  GIPS
  - **Efficiency** = sustained speed / peak speed =  $0.05 / 3.07 = 1.63\%$
- For the Fibonacci Computer with caching
  - Sustained speed =  $7/12 = 1.79$  GIPS
  - **Speedup** =  $1.79 \text{ GIPS} / 0.05 \text{ GIPS} = 35.8$
  - Efficiency = sustained speed / peak speed =  $1.79 / 3.07 = 58.3\%$
- Both have the same peak speed, but caching significantly improves real speed (sustained speed)

## 6.3 Parallel computing

- Also known as parallel processing
- What if one CPU is not enough?
  - What if we need 10 GIPS, 1 million GIPS, 1 trillion GIPS?
- Use multiple CPUs/processors/computers in one system
  - A processor having multiple CPUs is called a **multicore** processor
    - Each CPU is called a **core**



# Supercomputer examples

- Top500.org is a list ranking the world's fastest supercomputers
  - Maintained since 1993 by scientists in Europe and USA
  - Rank the 500 fastest supercomputers by their speeds in executing the Linpack benchmark
    - Speed = executed 64-bit floating-point operations per second (FLOPS)
- The main contributing factor of progress is parallel computing

**The Linpack benchmark** program for solving a system of linear equations using Gaussian elimination. It finds  $\mathbf{x}$  in  $\mathbf{Ax} = \mathbf{b}$ , where  $\mathbf{A}$  is an  $N \times N$  matrix, and  $\mathbf{x}, \mathbf{b}$  are two  $N$ -dimensional vectors. For  $N=3$ , we have

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \times \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix}$$

| Time of Test    | 1993                  | 2020            | 1993-2020 Growth Factor |
|-----------------|-----------------------|-----------------|-------------------------|
| Top-1 Name      | Thinking Machine CM-5 | Fujitsu Fugaku  | N/A                     |
| Problem Size    | N = 52,224            | N = 20,459,520  | 392                     |
| Speed           | 59.7 GFlop/s          | 415,530 TFlop/s | 6,960,302               |
| Clock Frequency | 32 MHz                | 2.2 GHz         | 69                      |
| Parallelism     | 1,024 cores           | 7,299,072 cores | 7,128                   |
| Memory          | 32 GB                 | 4,866,048 GB    | 152,064                 |
| Power           | 96.5 KW               | 28,334.5 KW     | 294                     |
| Cost            | US \$30 million       | US \$1 billion  | 33                      |